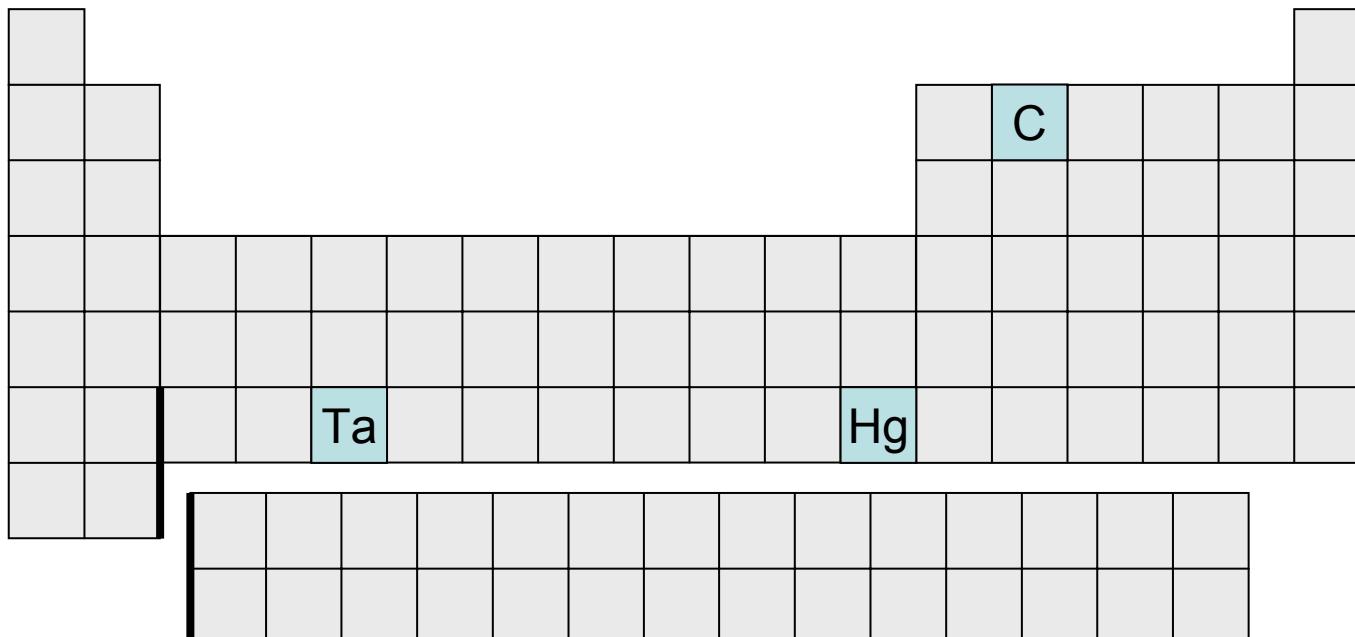


Neutrino Factory Target Yield Considerations

[Click to view with less target stuff](#)

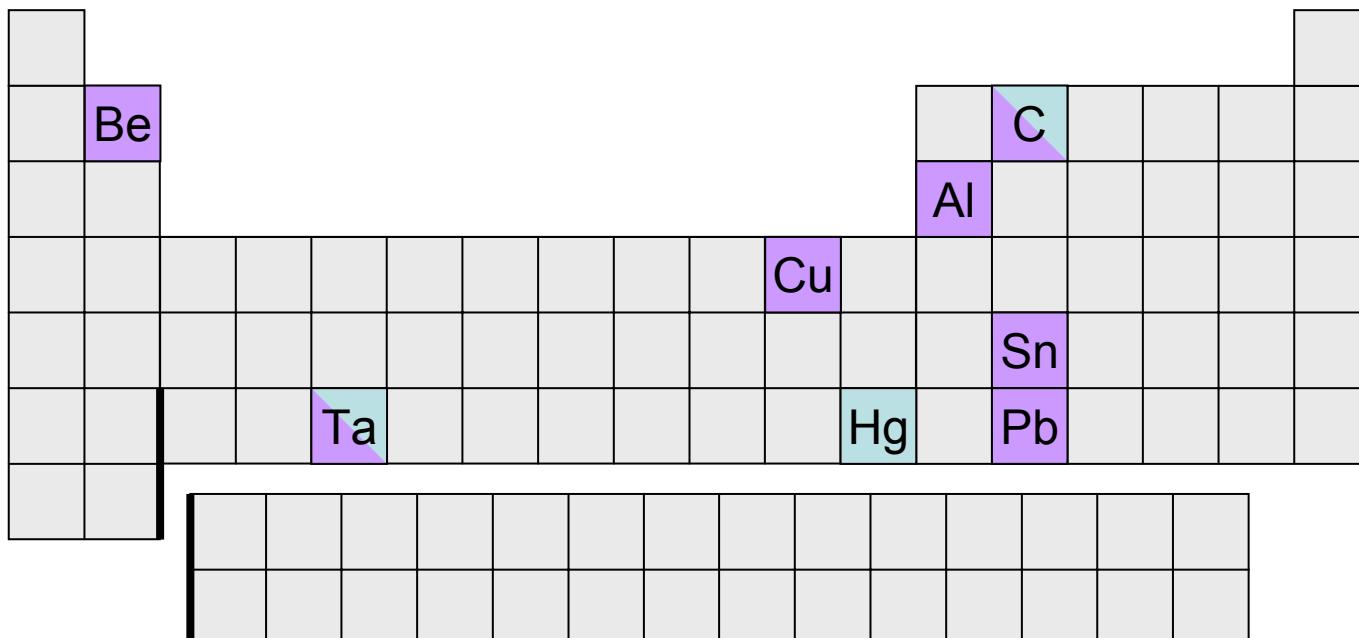
Intermediate Z Element Needed

- Previously, results for Ta, Hg and C
- C behaviour was very different from others
- C is in P2, the others are in P6

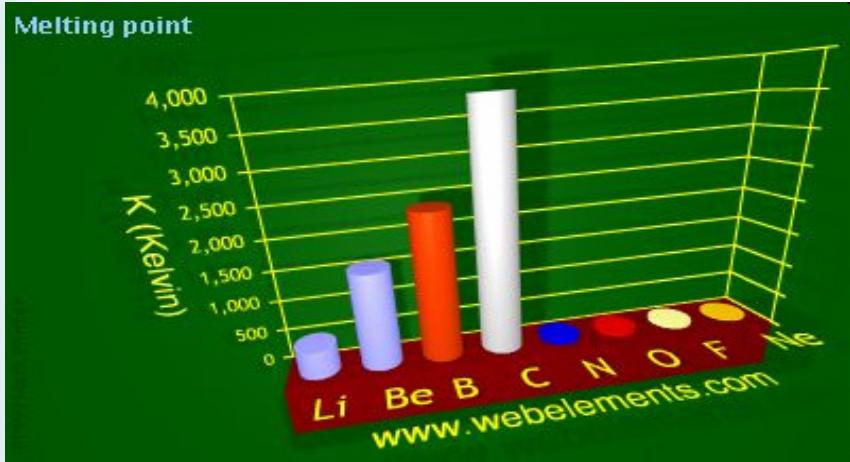


Compare: HARP Elements

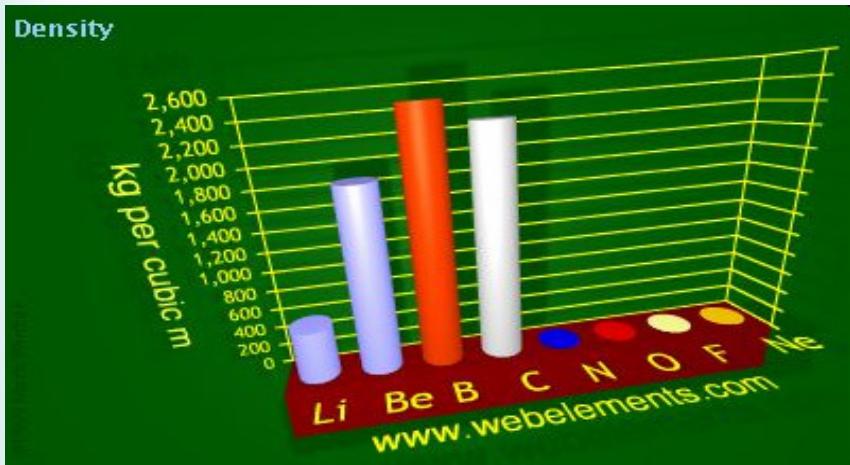
- P3: Al
- P4: Cu
- P5: Sn
- Want to compare with data
- Sensible target element
 - High melting point, density



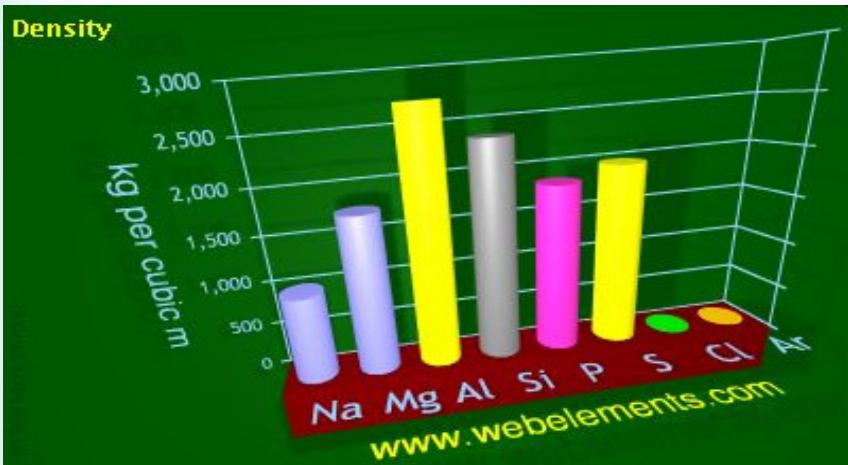
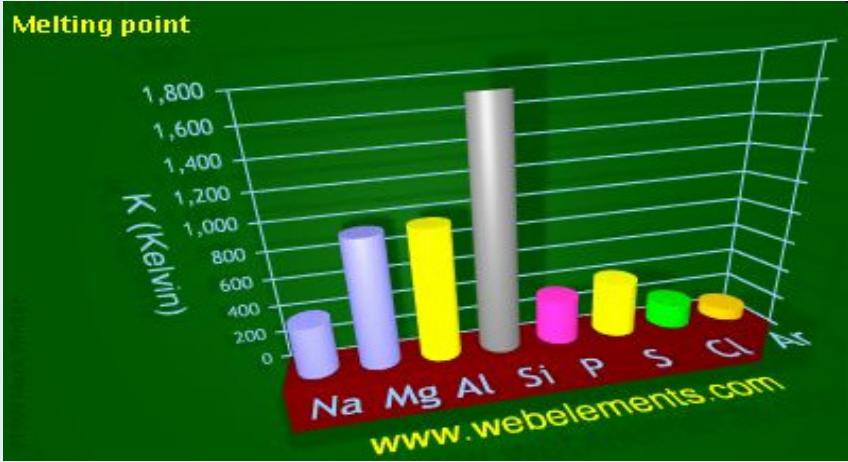
Period 2 Elements



- Carbon clearly wins
- Boron and beryllium not so bad
- HARP has Be and C
- None of these densities are very high: require long targets



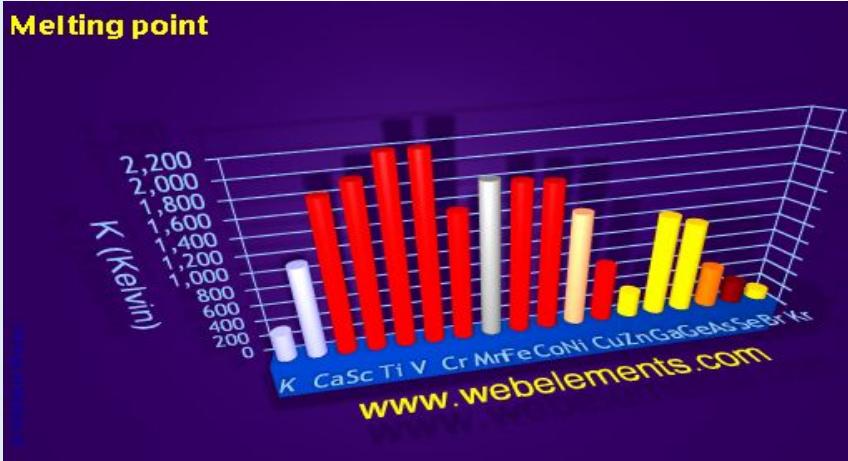
Period 3 Elements



- Silicon looks best
- Everything else has a useless melting point
- HARP has aluminium
- Densities no higher than before
- I think P3 is a non-starter

Period 4 Elements

Melting point

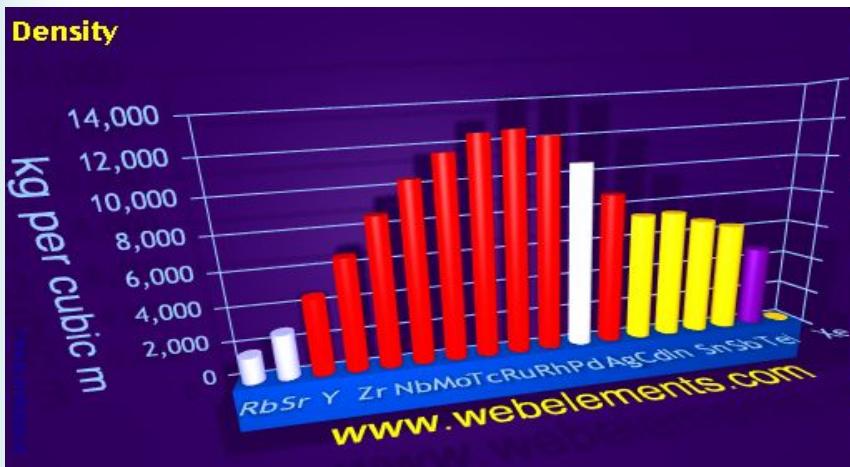
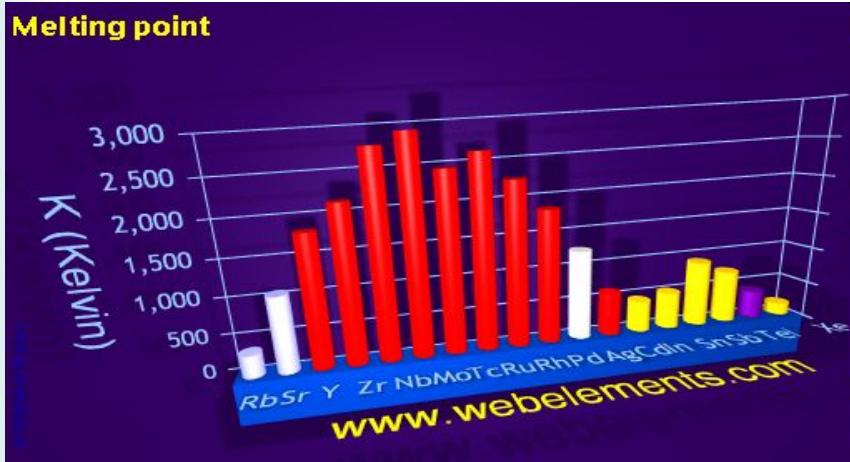


Density



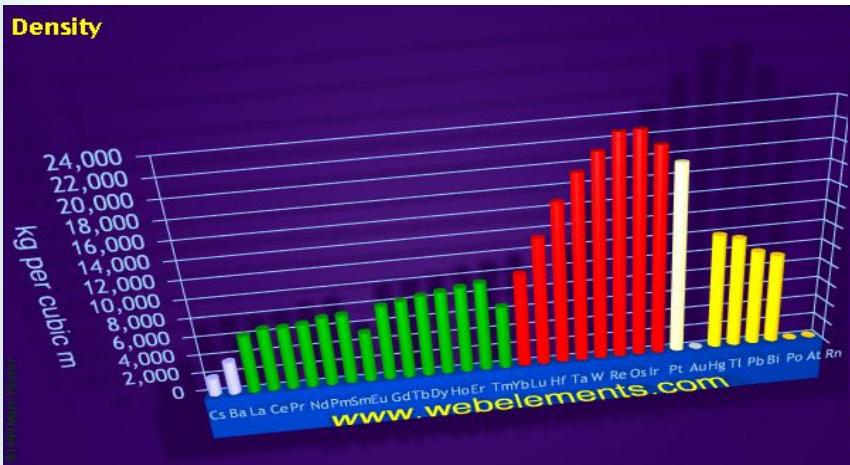
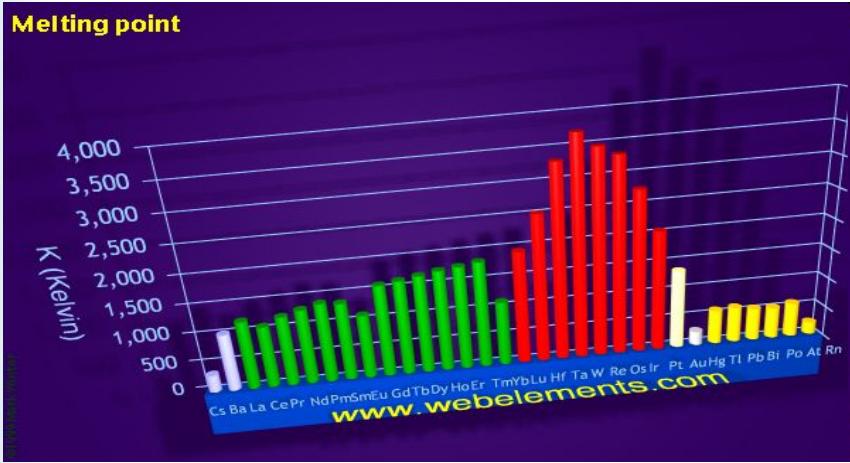
- Transition metal melting points and densities are better
- HARP's Cu has high density and moderate melting point
- Also about half-way (logarithmically) between C and Ta/Hg

Period 5 Elements



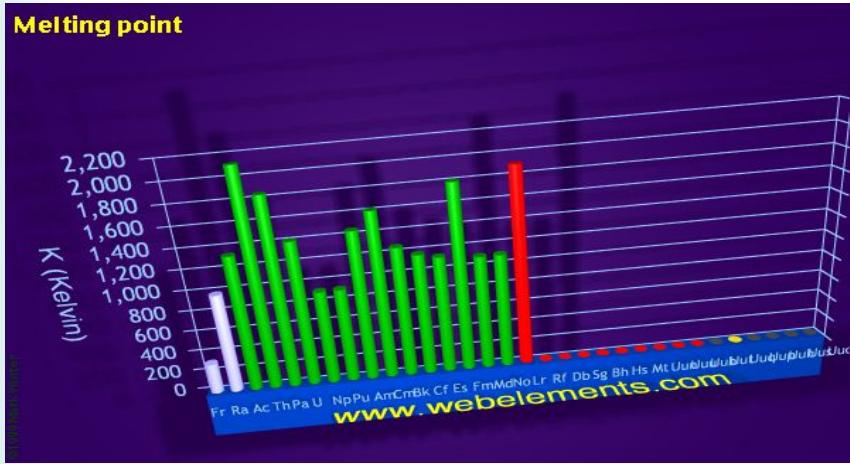
- Melting points and densities continue to increase
- HARP's tin is not good for our target!
- Plenty of workable choices in transition block, if needed

Period 6 Elements

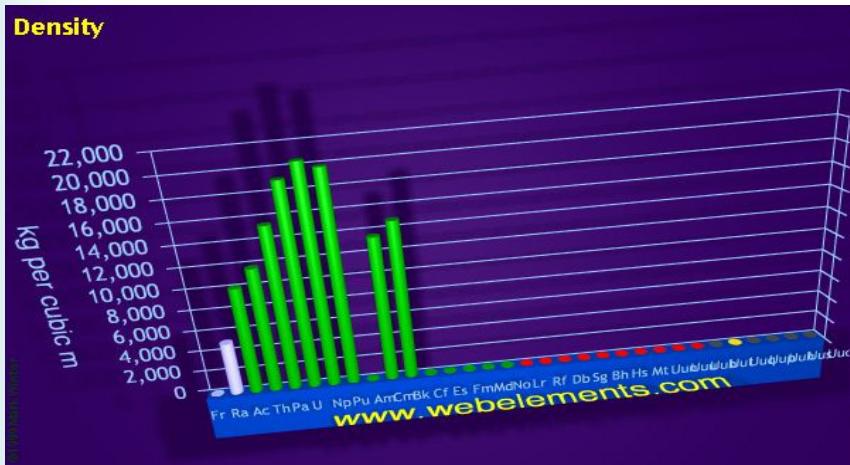


- Transition metals here have the highest values in the table
- Hence the choice of Ta in the first place
- Hg is obviously a special case

Period 7 Elements



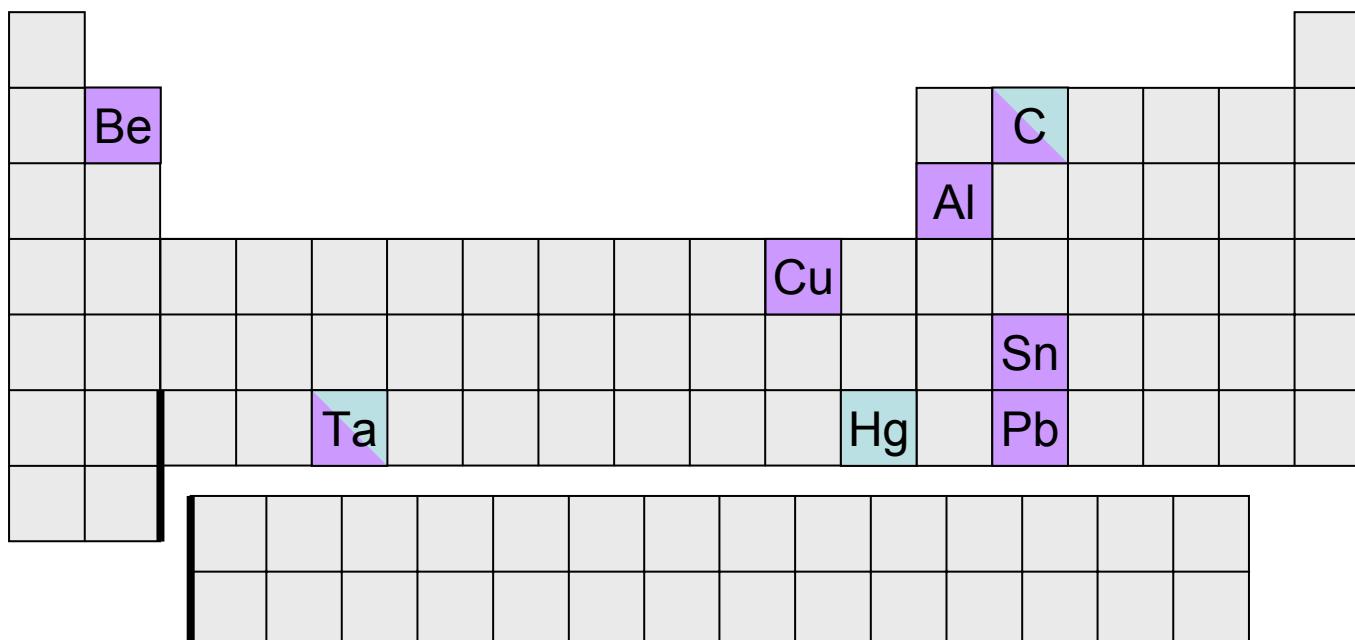
- Thorium → uranium are OK for very-high-Z if needed
 - Most of the rest are radioactive



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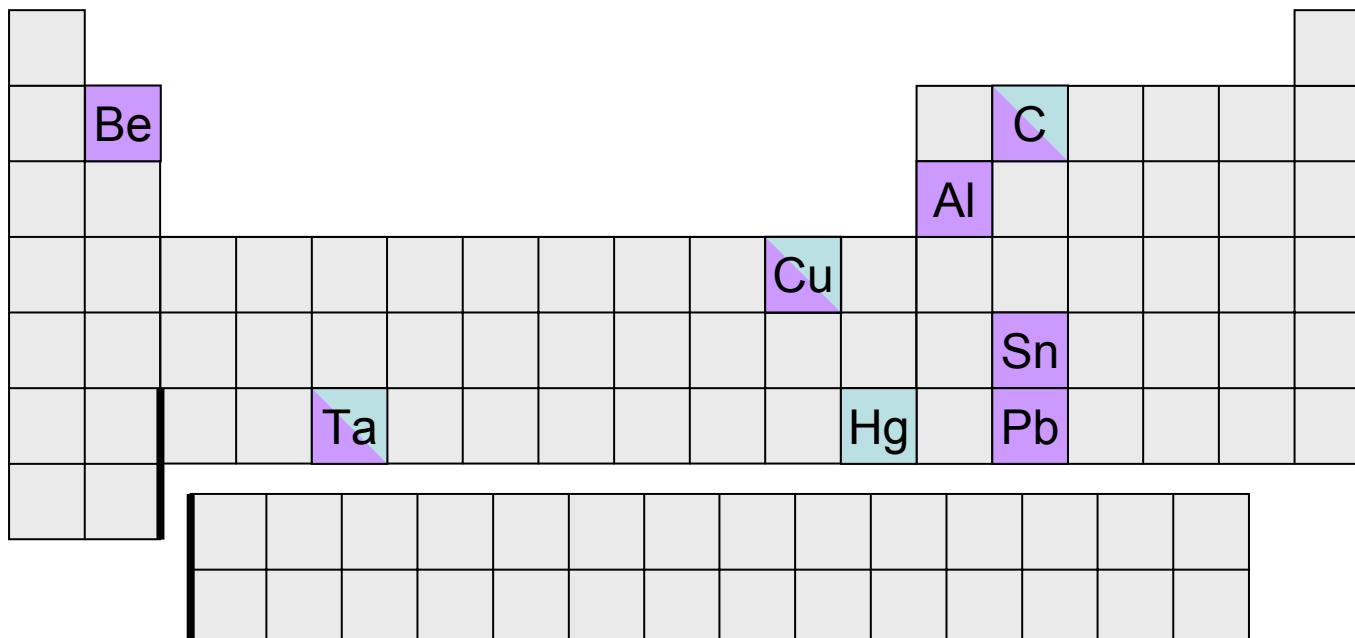
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Scaling of Cylinder Length

- Proportional to hadronic interaction length

Element	Interaction length (cm)	Equivalent to 20cm Ta
Ta	11.18	20cm
Hg	13.95	25cm
C	36.92	66cm
Cu	15.16	27cm
W	9.54	17cm

Harold Kirk found
~60cm is optimal

Data from <http://www.slac.stanford.edu/comp/physics/matprop.html>

Summary Statistics ($\pi^\pm/p.\text{GeV}$)

- “Total Pion Yield” = all pions (of one sign) emitted from the *rod surface*
- “Captured Yield” = these weighted by survival probability in (p_L, p_T) space
 - Survival end of (UK) phase rotation into energy band $180 \pm 23\text{MeV}$ of cooling ring
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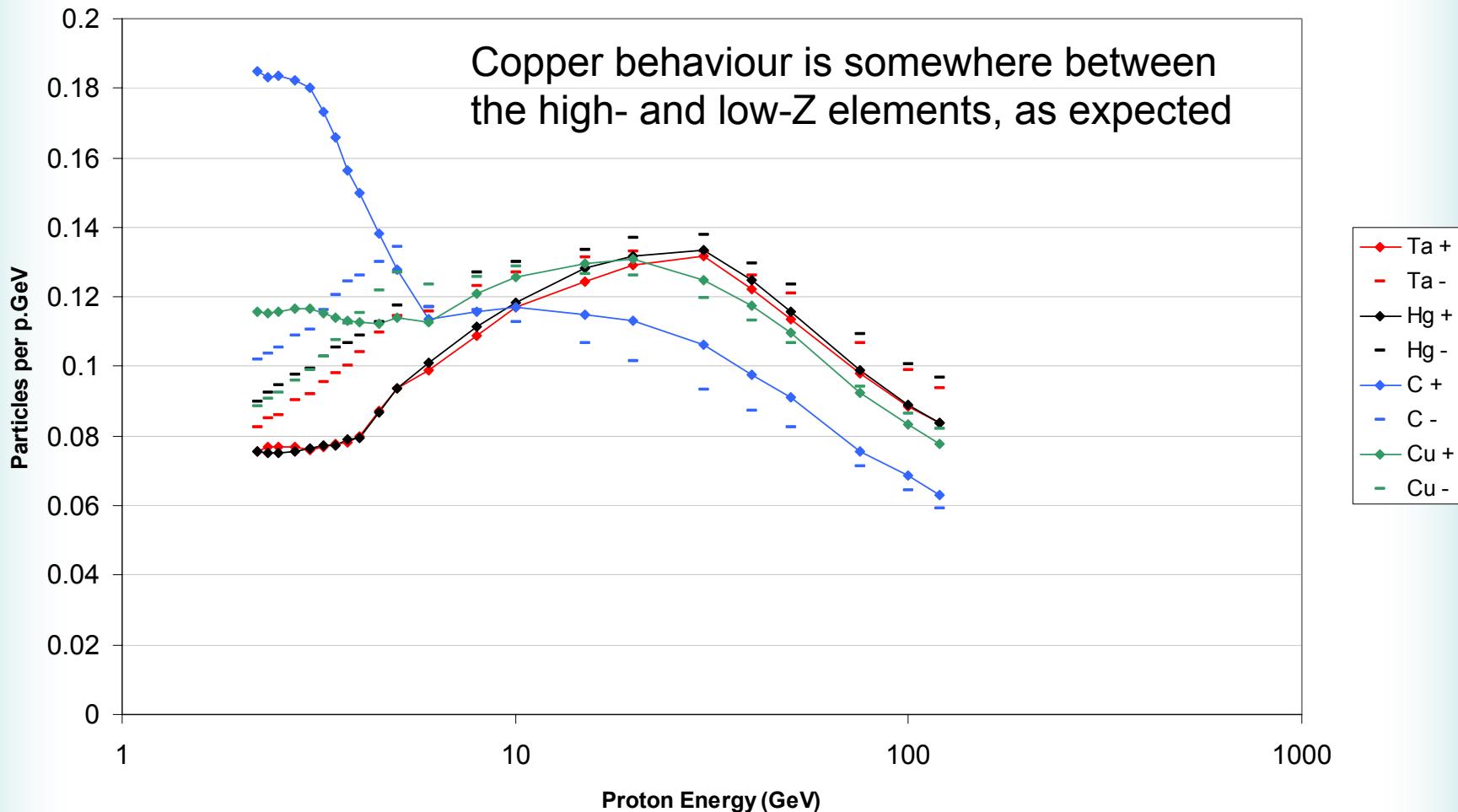
Decay modes of K⁺ from PDG

- For E>3GeV, kaons add to the production
 - “A kaon is equivalent to ~1.06 pions”

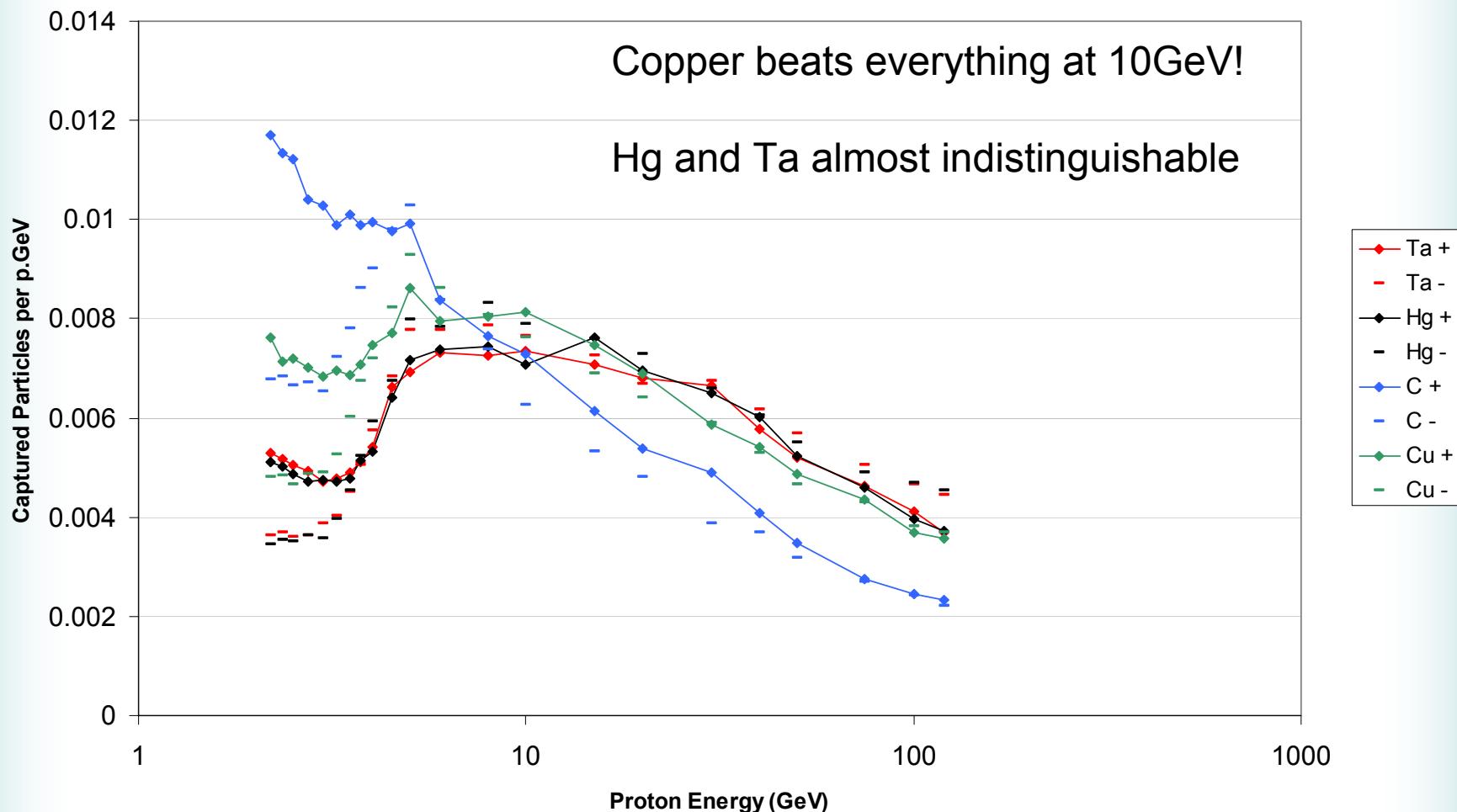
Mode	Fraction (error)	π^\pm and μ^\pm	Expected
$\mu^+ \nu_\mu$	63.39% 0.18%	1	0.6339
$\pi^0 e^+ \nu_e$	4.93% 0.07%	0	0
$\pi^0 \mu^+ \nu_\mu$	3.30% 0.06%	1	0.033
$\pi^+ \pi^0$	21.03% 0.13%	1	0.2103
$\pi^+ \pi^0 \pi^0$	1.76% 0.02%	1	0.01757
$\pi^+ \pi^+ \pi^-$	5.59% 0.05%	3	0.1677

Mean eventual muons: **1.06247**

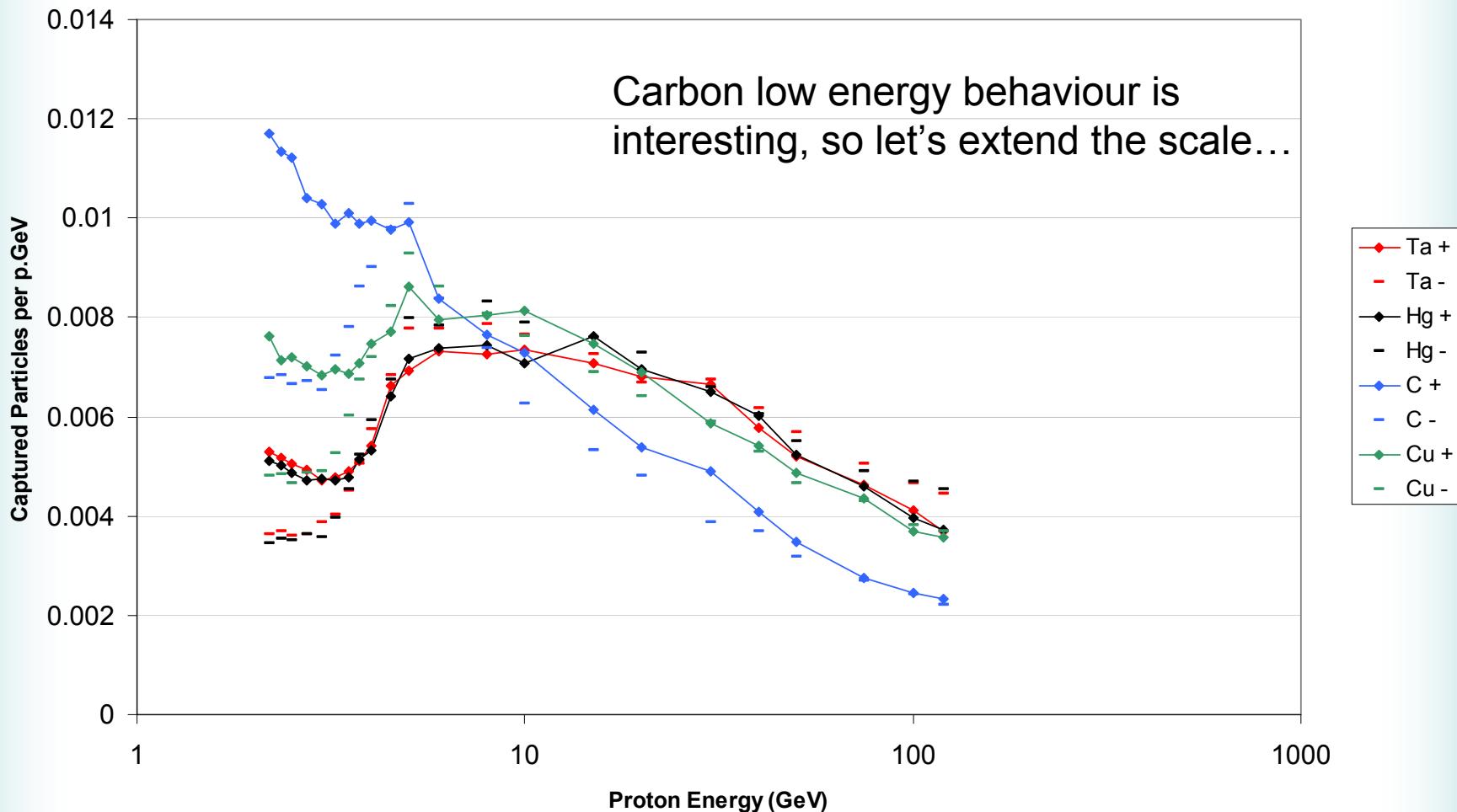
Results: Total Pion Yield



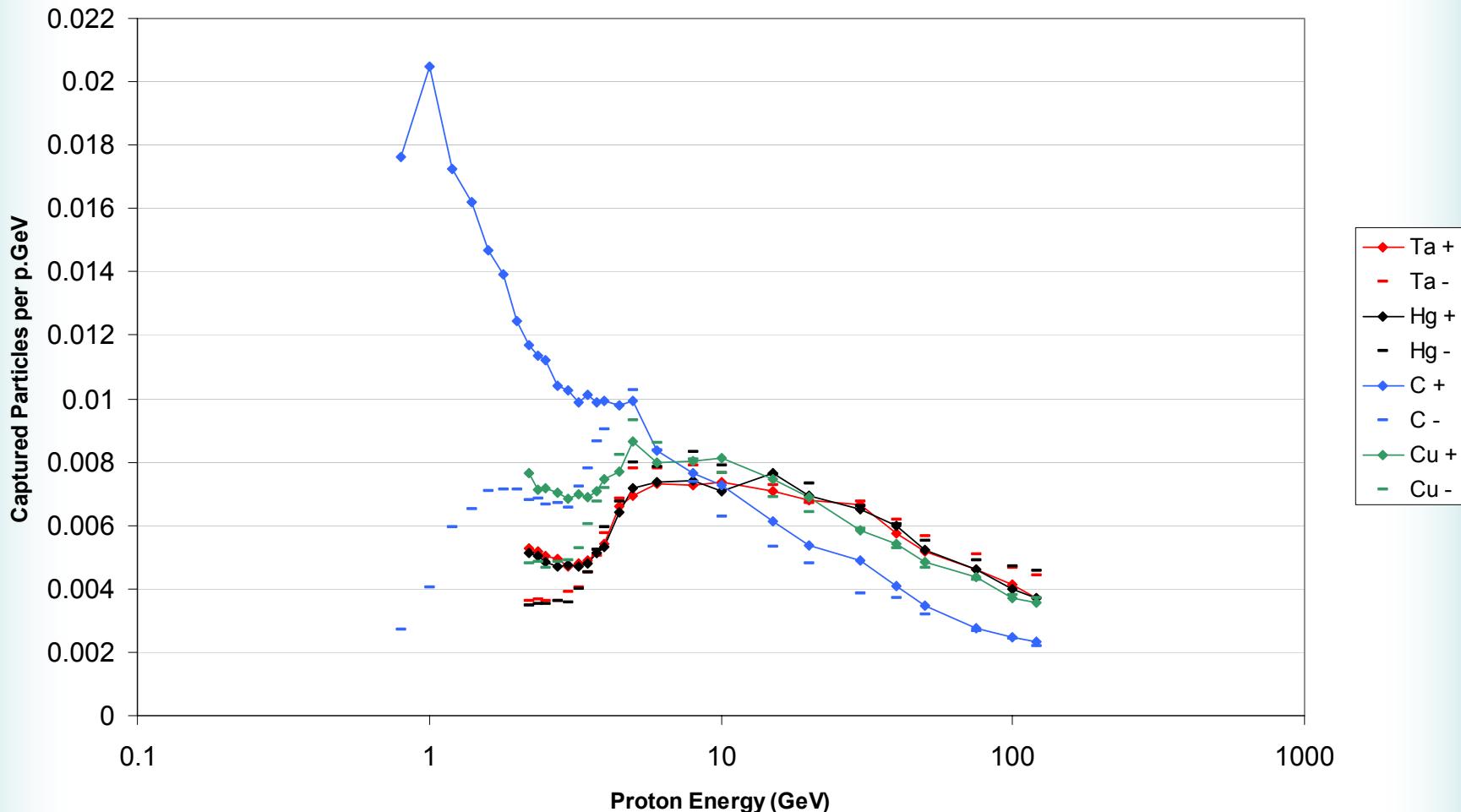
Results: Captured Yield



Results: Captured Yield



Results: Captured Yield



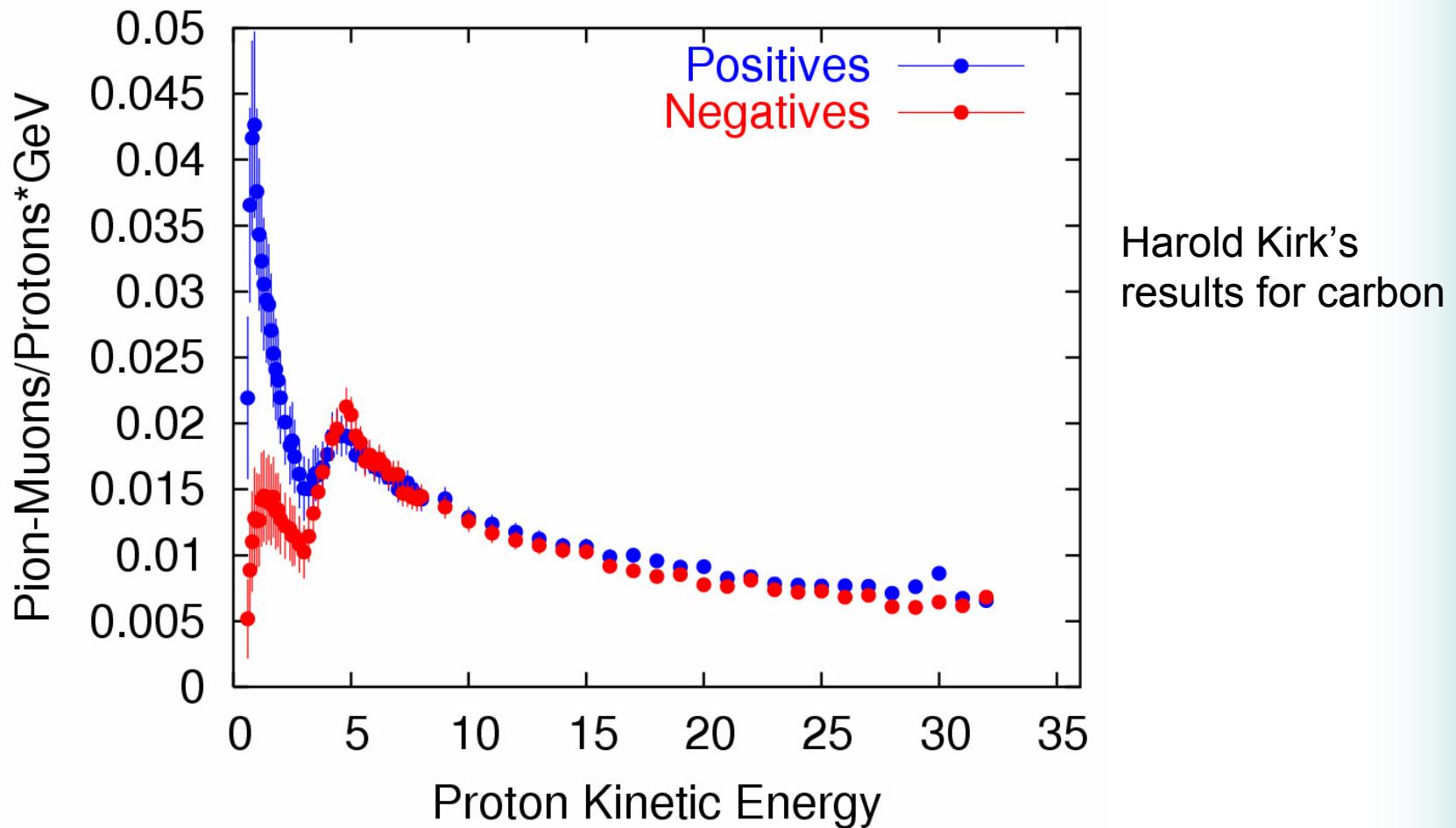
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Scoping Study meeting, April 2006

Observations

- The carbon peak at 1GeV is huge, but can you build a proton driver at that energy?
- Low energy behaviour is increasingly asymmetrical in sign for low Z
 - Proton charge manifests excess of π^+
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Comparison with FS2, ICOOL

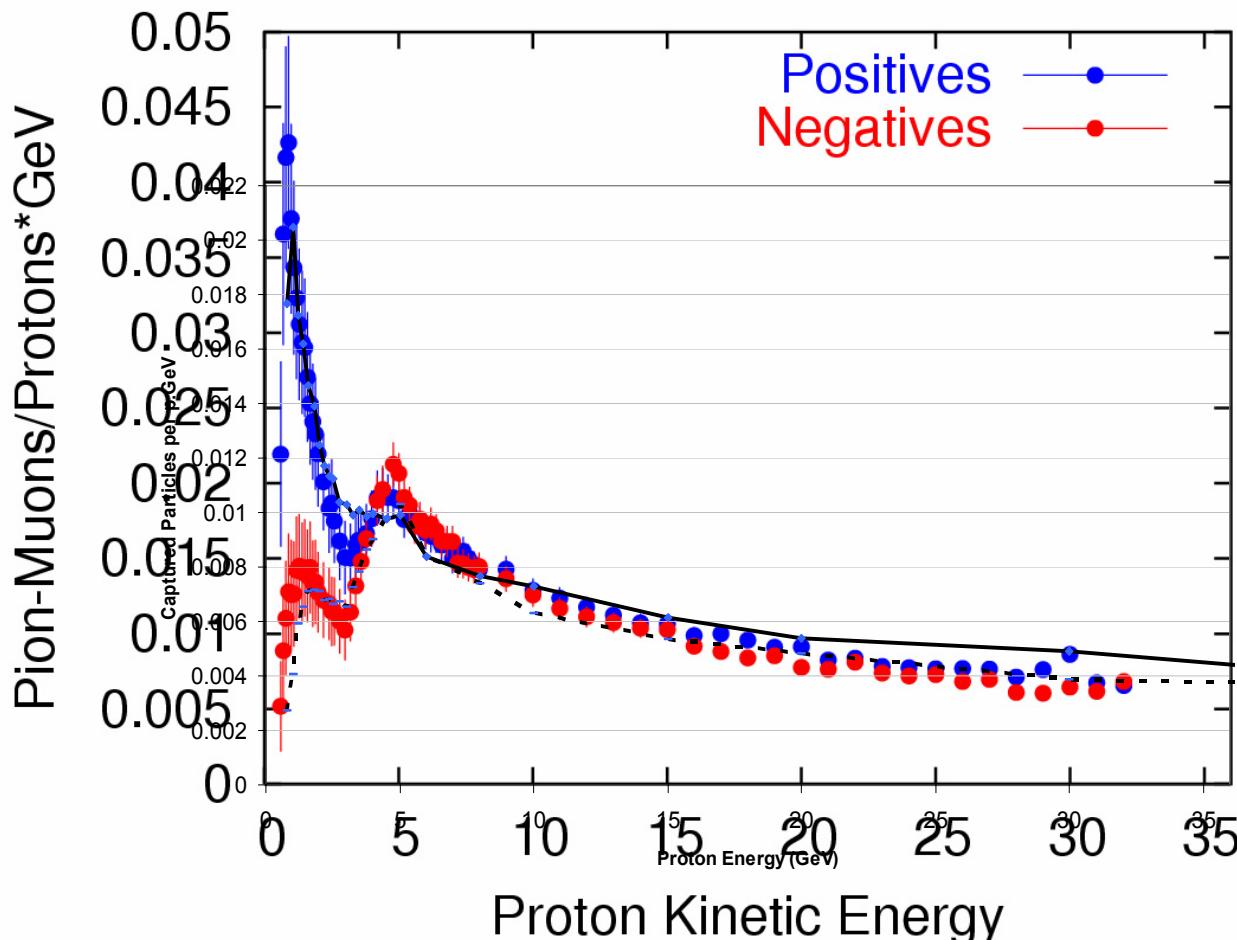
MARS13



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Comparison with FS2, ICOOL

MARS13



Harold Kirk's
results for carbon

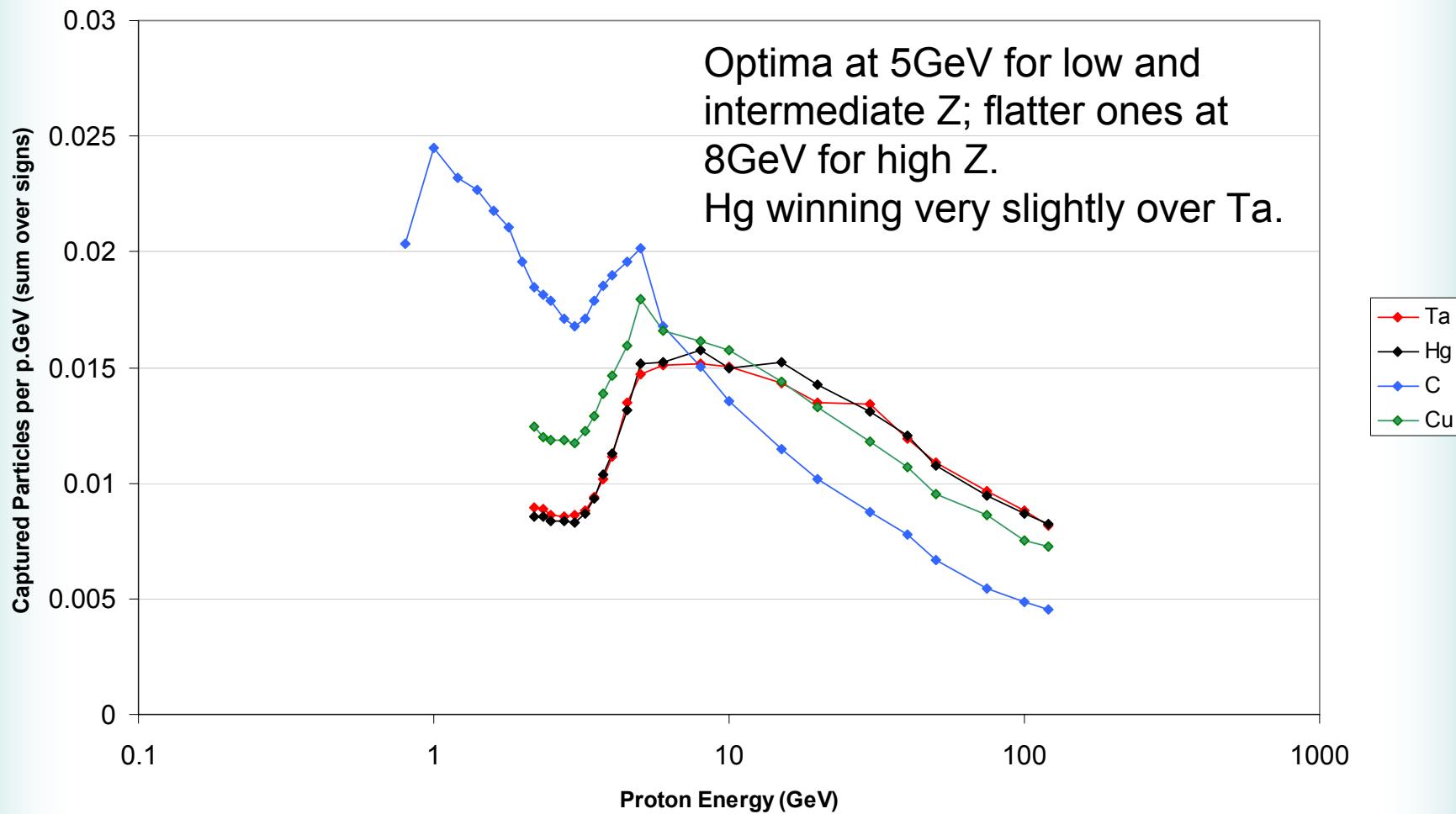
C +
C -

...are a similar
shape to my results,
with a scaling due to
using more efficient
RF capture

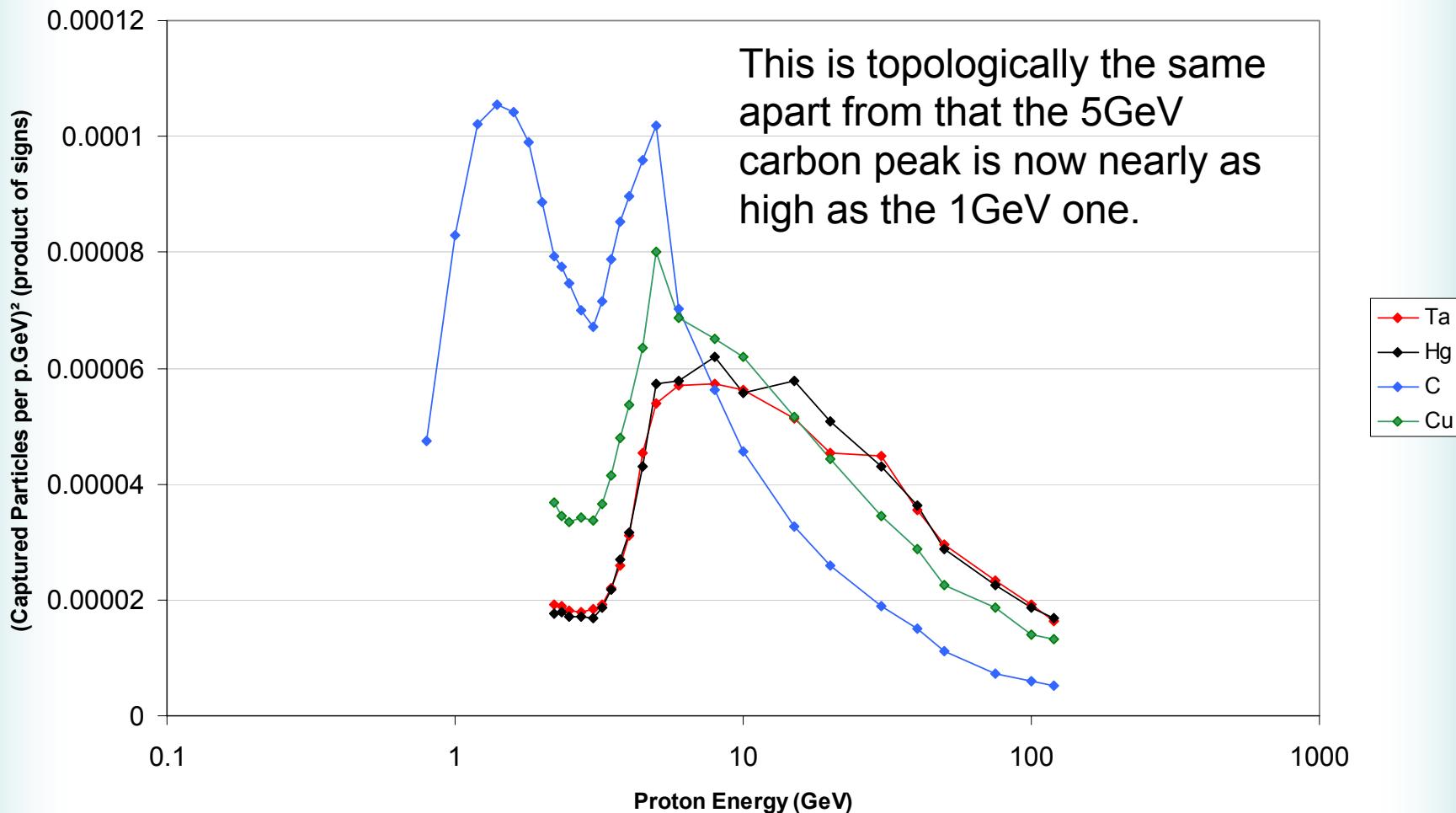
Figure of Merit: $\mu^+ + \mu^-$ or $\mu^+ \times \mu^-$?

- For the muon collider they should multiply
- For the neutrino factory, it depends on the physics goals
 - Experiments that test matter-antimatter asymmetry would require both signs
 - Detectors may be more sensitive to one sign than the other, giving an asymmetric function
- I will graph both + and \times cases for interest

Captured Yield Sum



Captured Yield Product



Pion Reabsorption (future work)

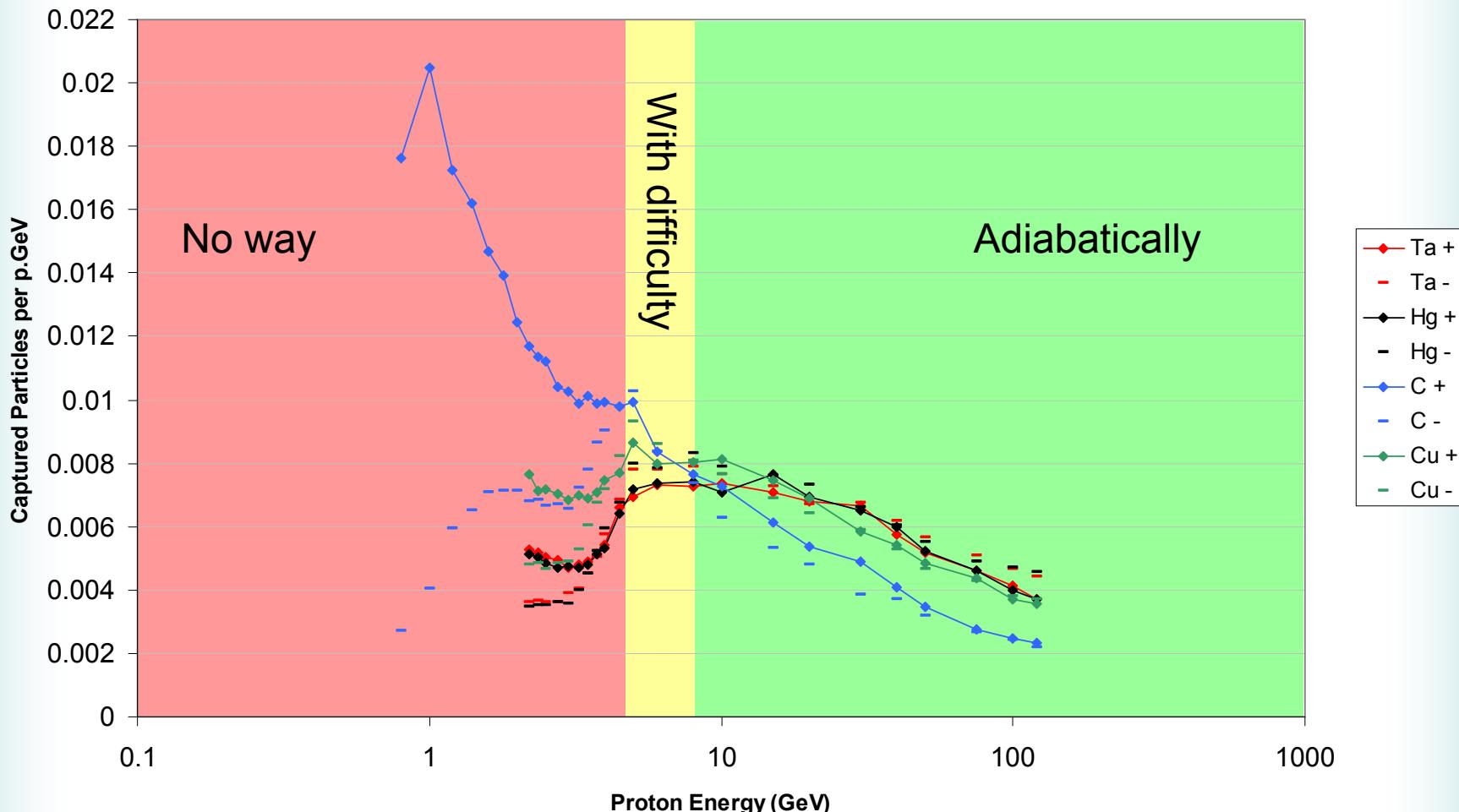
- It might be worth re-running MARS with a 20T field in the solenoid bore and collecting the pions at the endplane, to include this effect
- Could be significant in long, low-Z targets
- A rough model for manual tracking can also be obtained by extracting an “absorption length” for pions in material

Absorption Length Estimate

- MARS15 was run for pions entering a block of tantalum, surviving particles logged at various Z-planes and an exponential decay fit to the data

Energy	π^+ length	π^- length
100MeV	82mm	65mm
300MeV	107mm	106mm
1GeV	139mm	159mm

Feasibility of “1ns” Bunches



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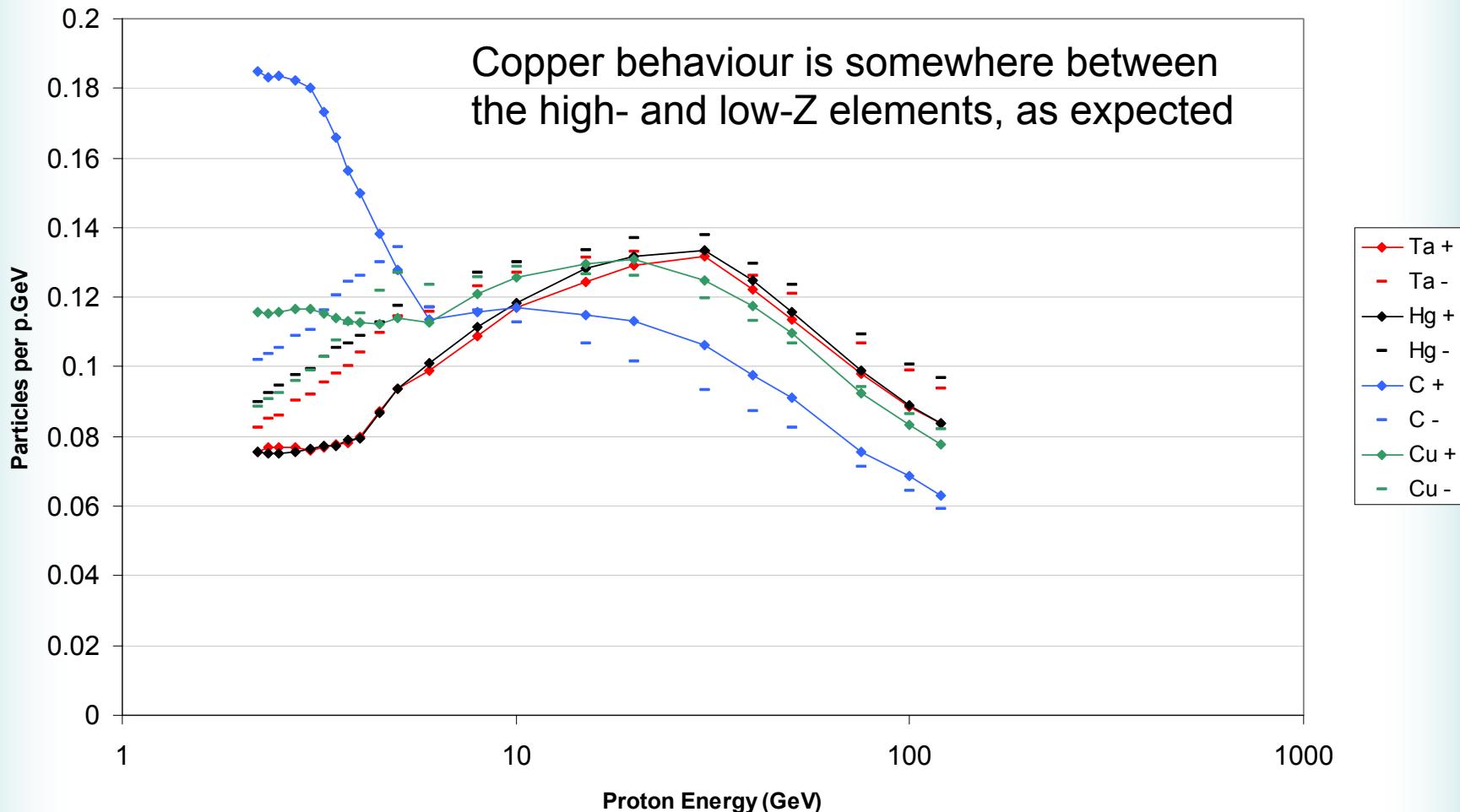
Higher Energies than 10GeV

- Going from 10GeV to 30GeV
 - Loses 10-12% yield with a high-Z target
 - Assuming fixed power (unrealistic?)
 - Re-optimising the front end for another energy tends to give small gains of order 3%
- Going from 10GeV to 50GeV
 - Loses 25-30% yield
 - This cannot be ignored so easily

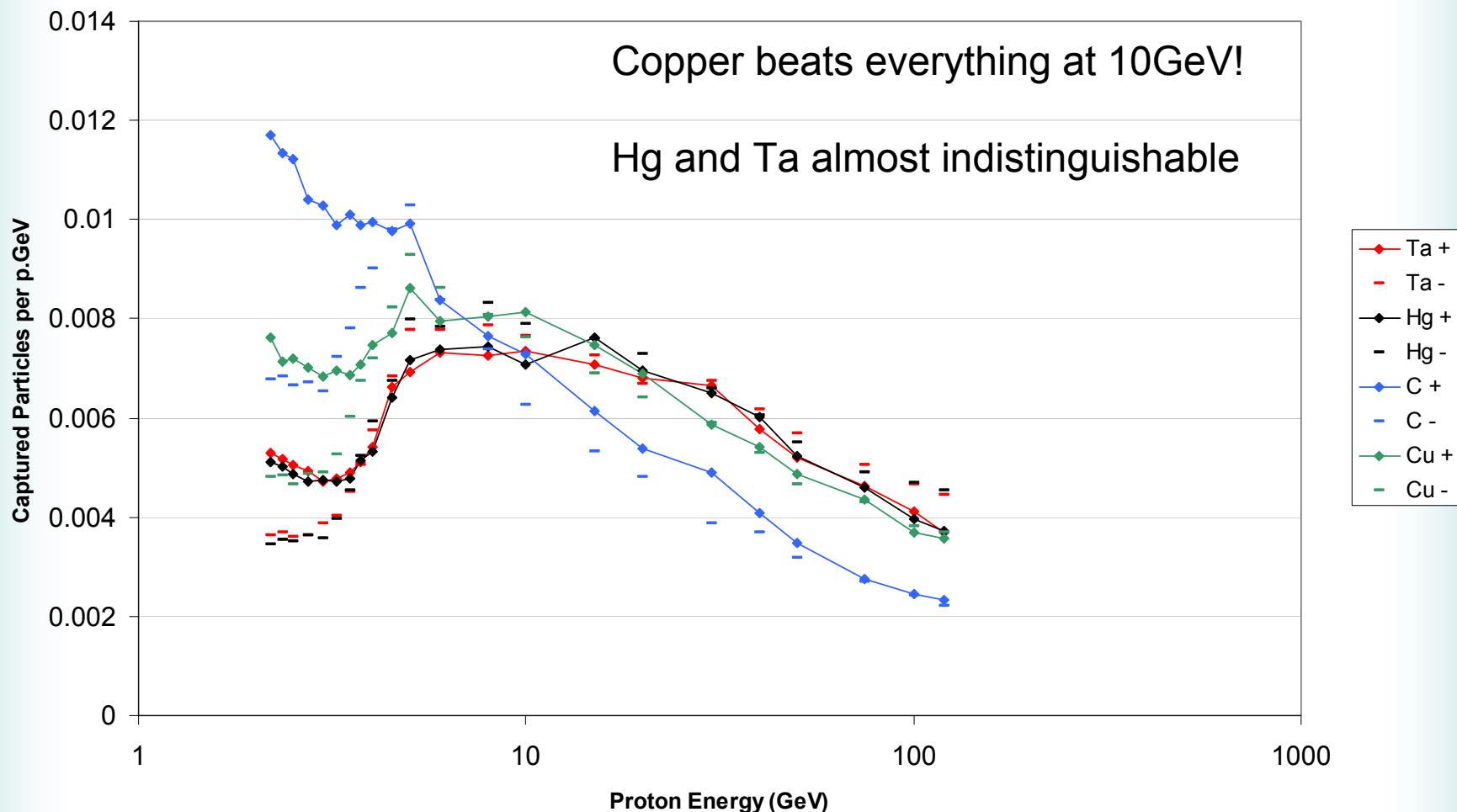
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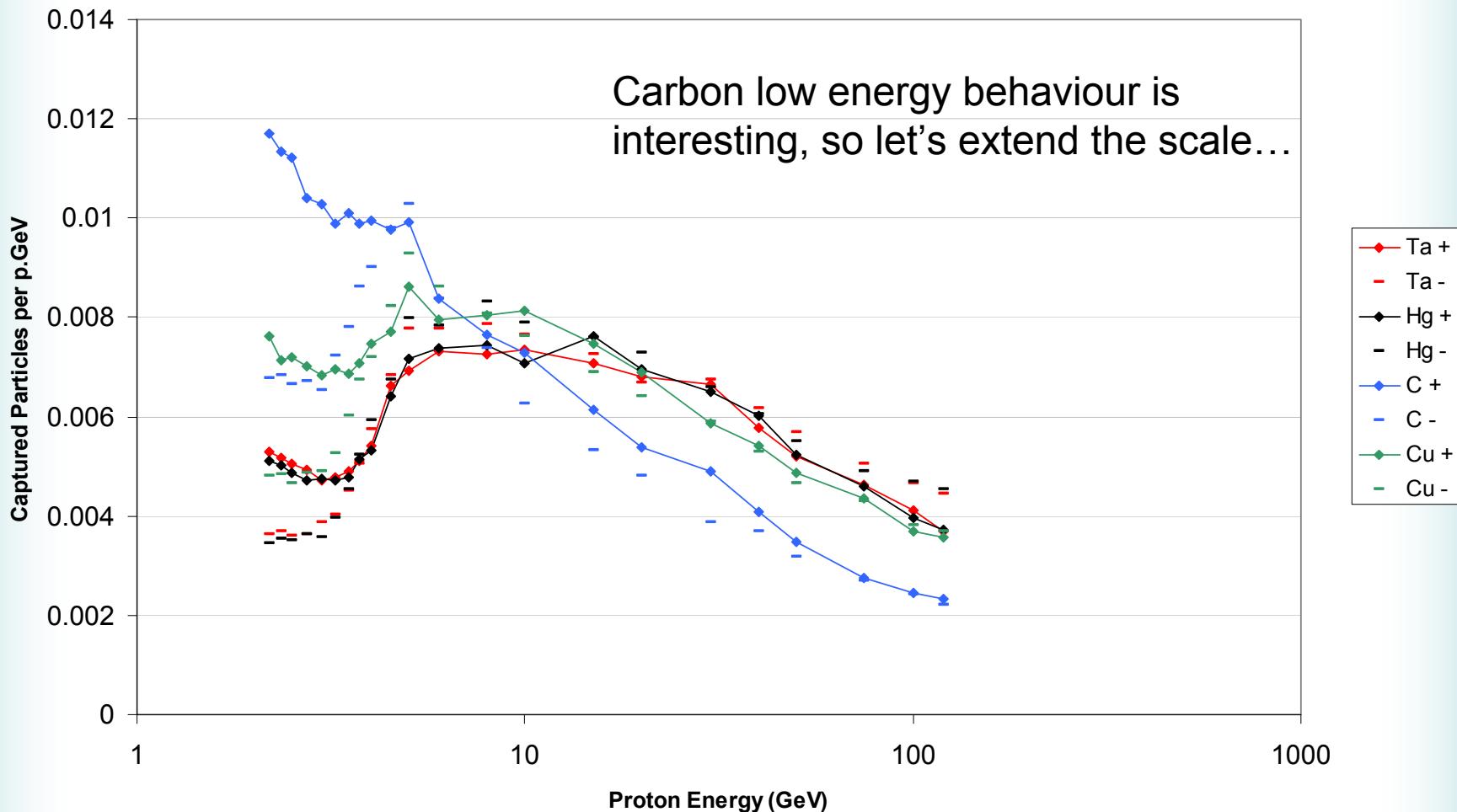
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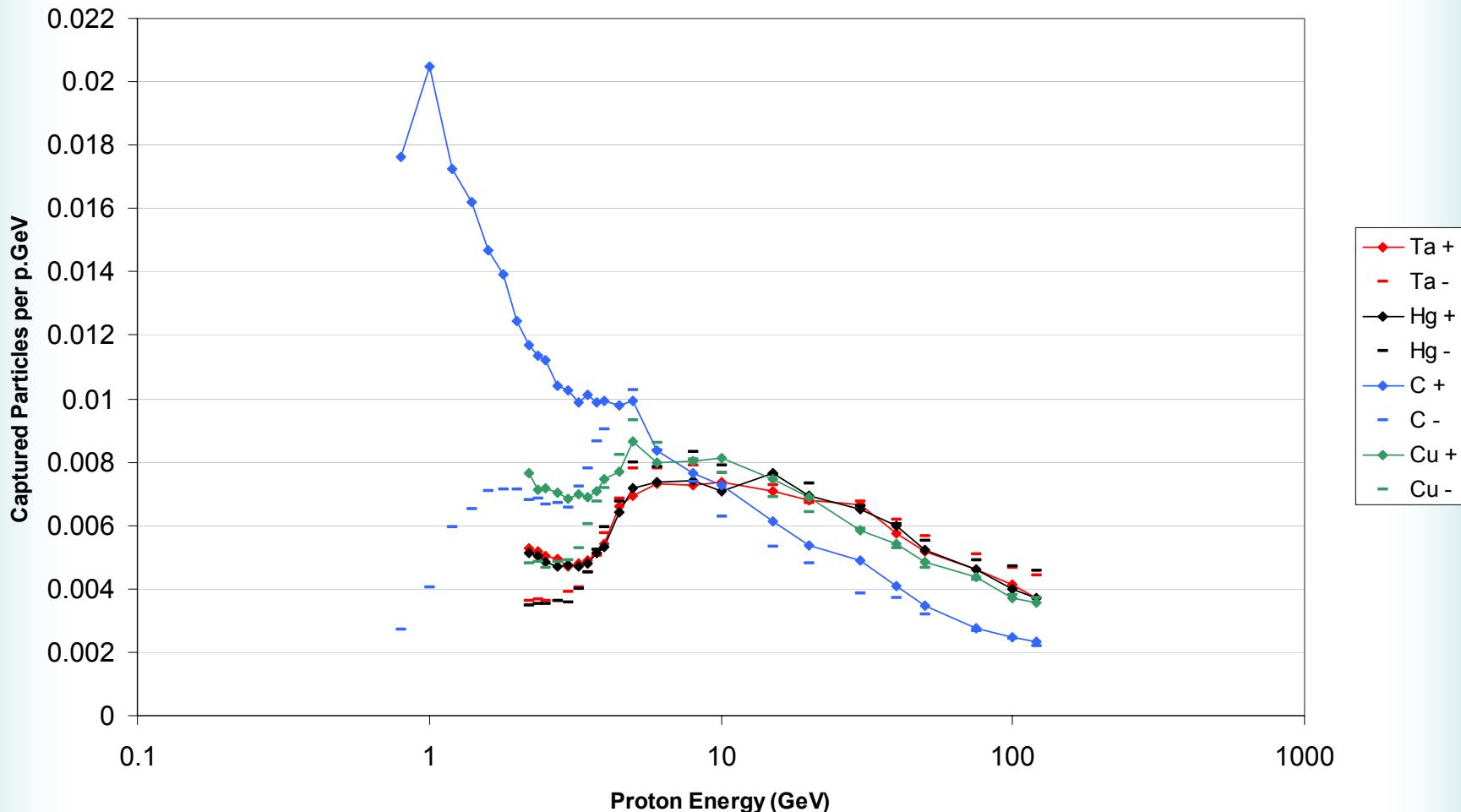
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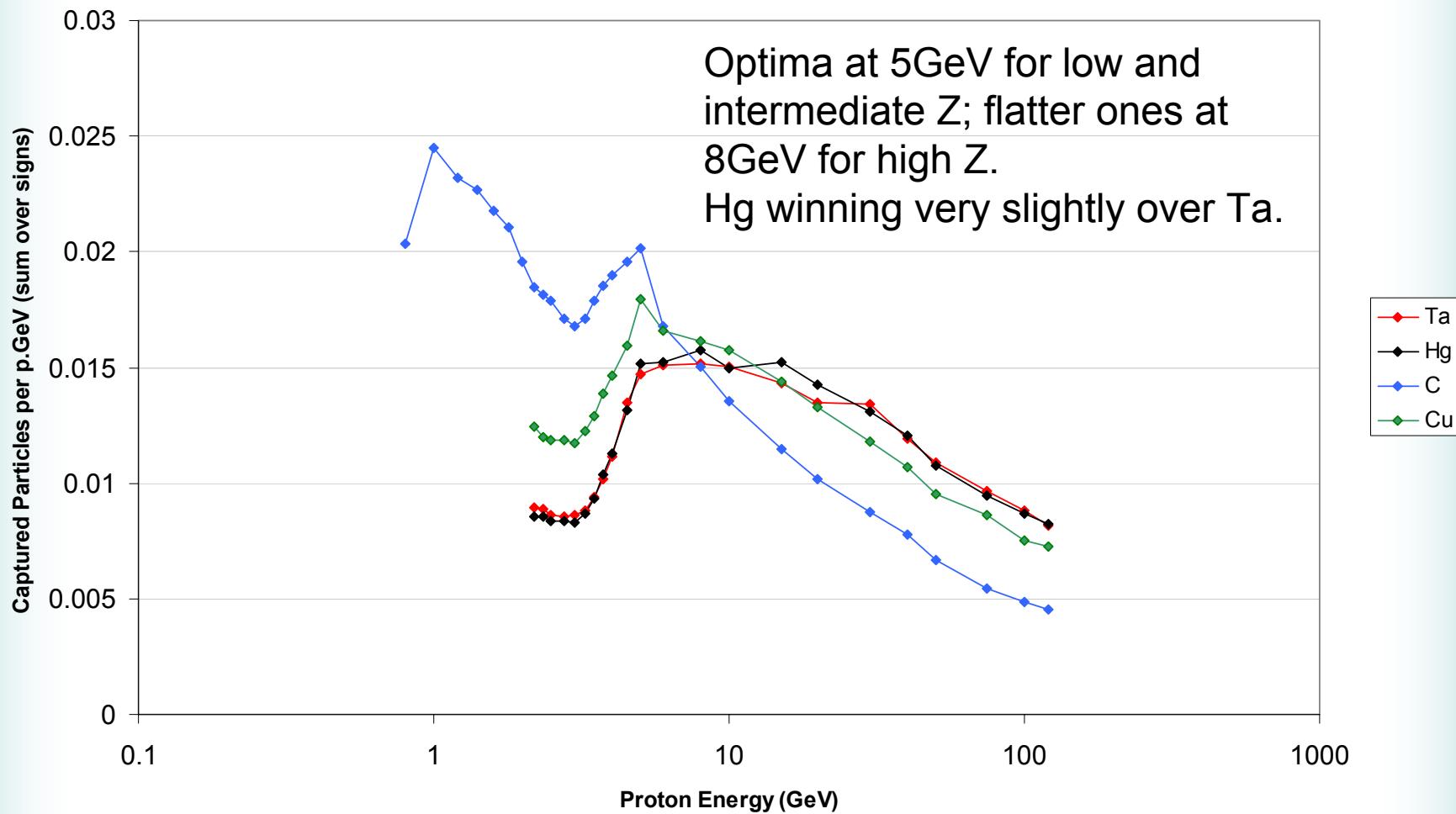
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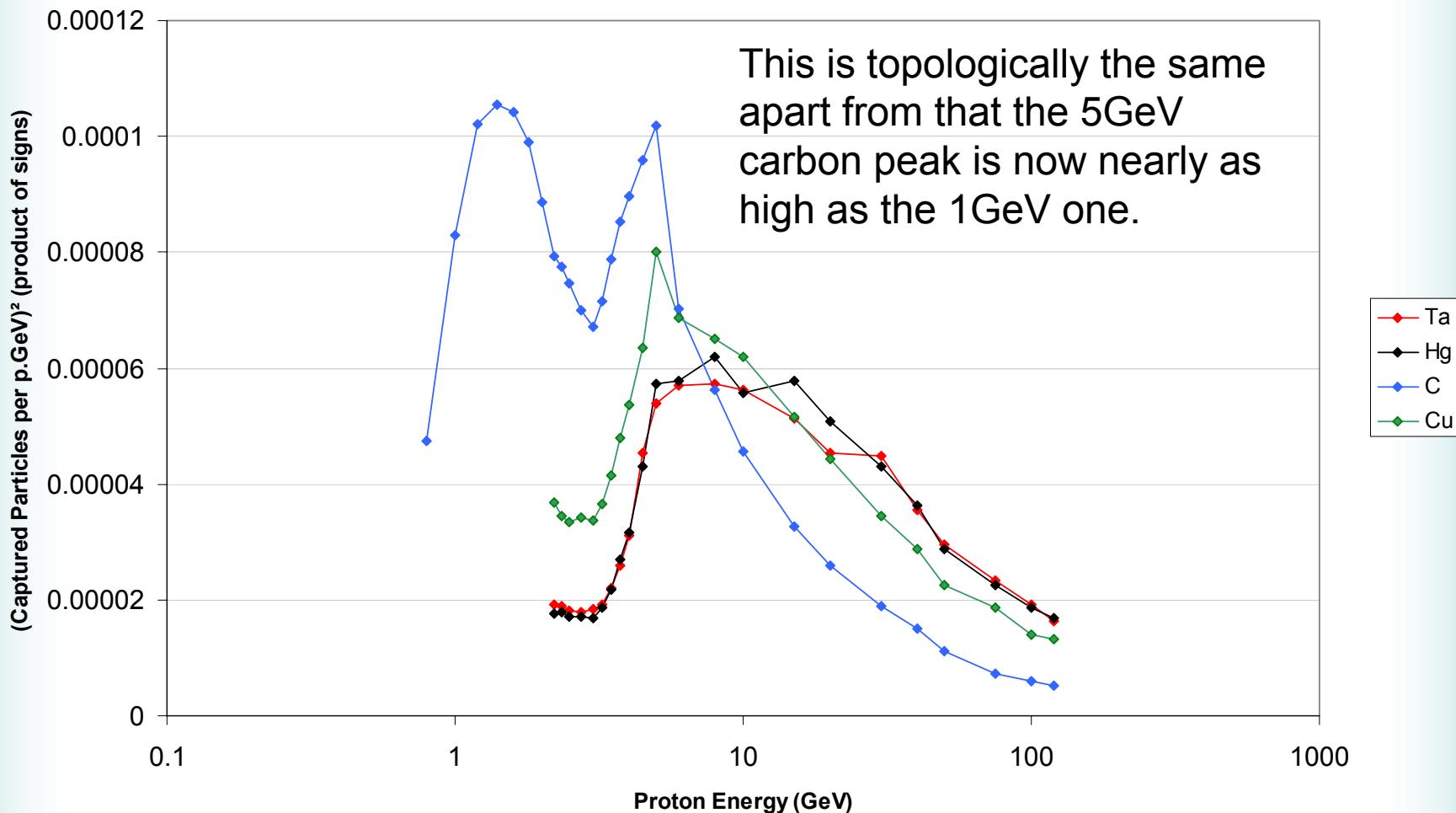
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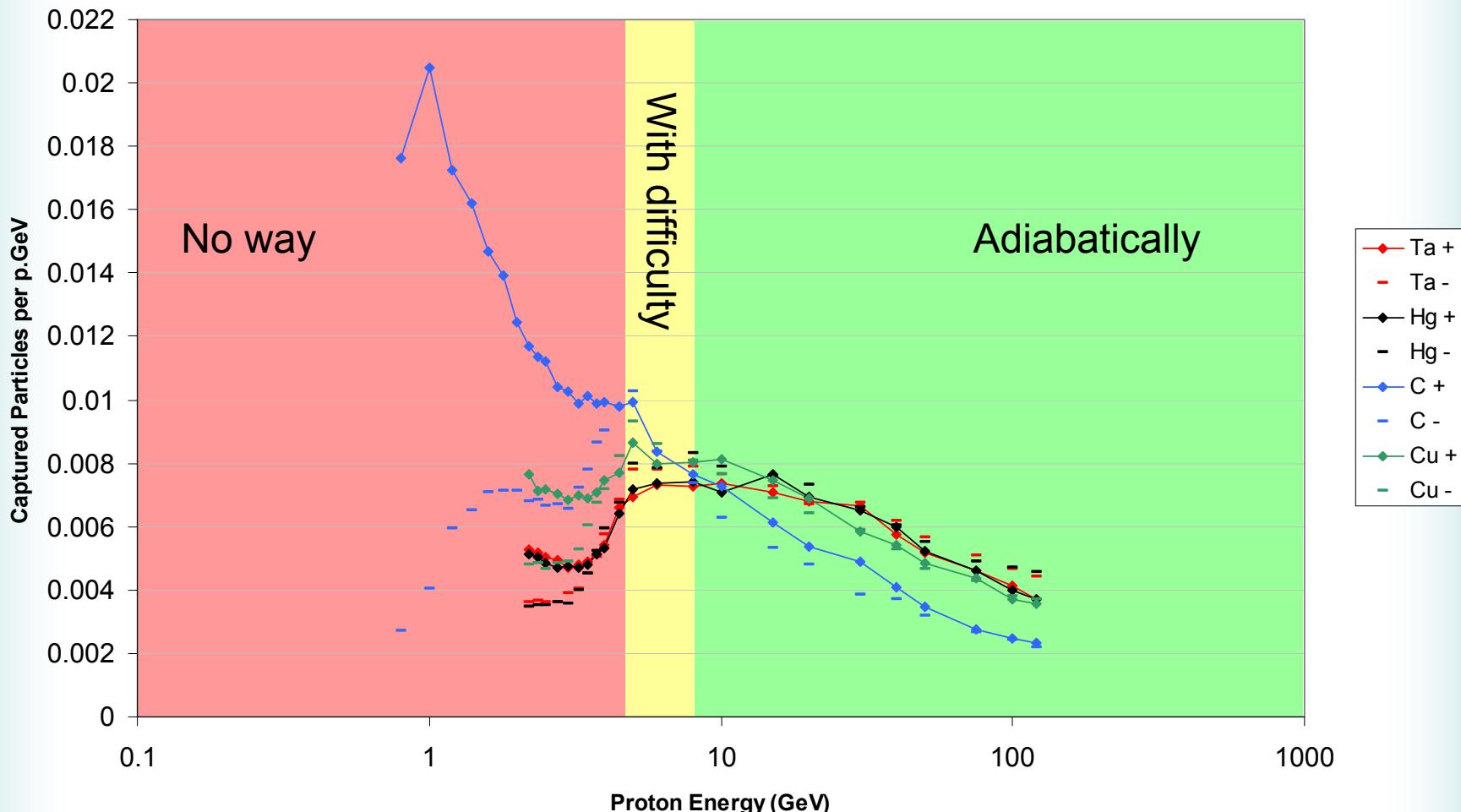
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