

MUON TARGET STUDIES: TAPERED CAPTURE SOLENOID

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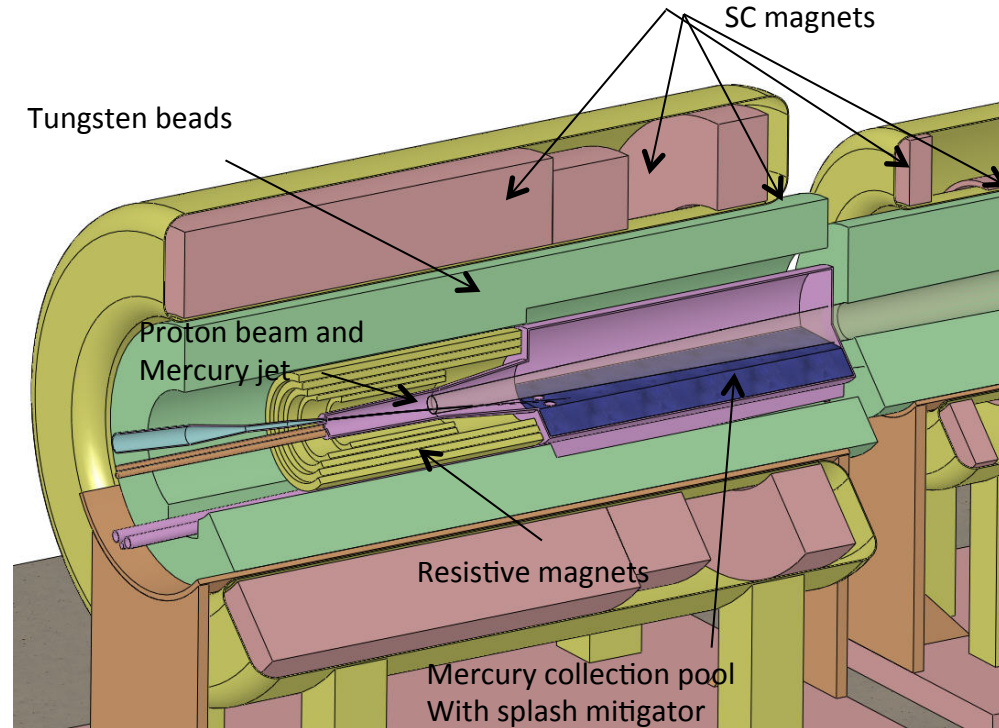
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OVERVIEW

- Target layout
- Current baseline parameters
- Solenoid Taper field calculations
- MARS simulation setup
- Tracking through FE with ICOOL
- Muon count
- Transverse position & Momentum distribution
- Conclusion

TARGET SYSTEM CURRENT BASELINE DESIGN

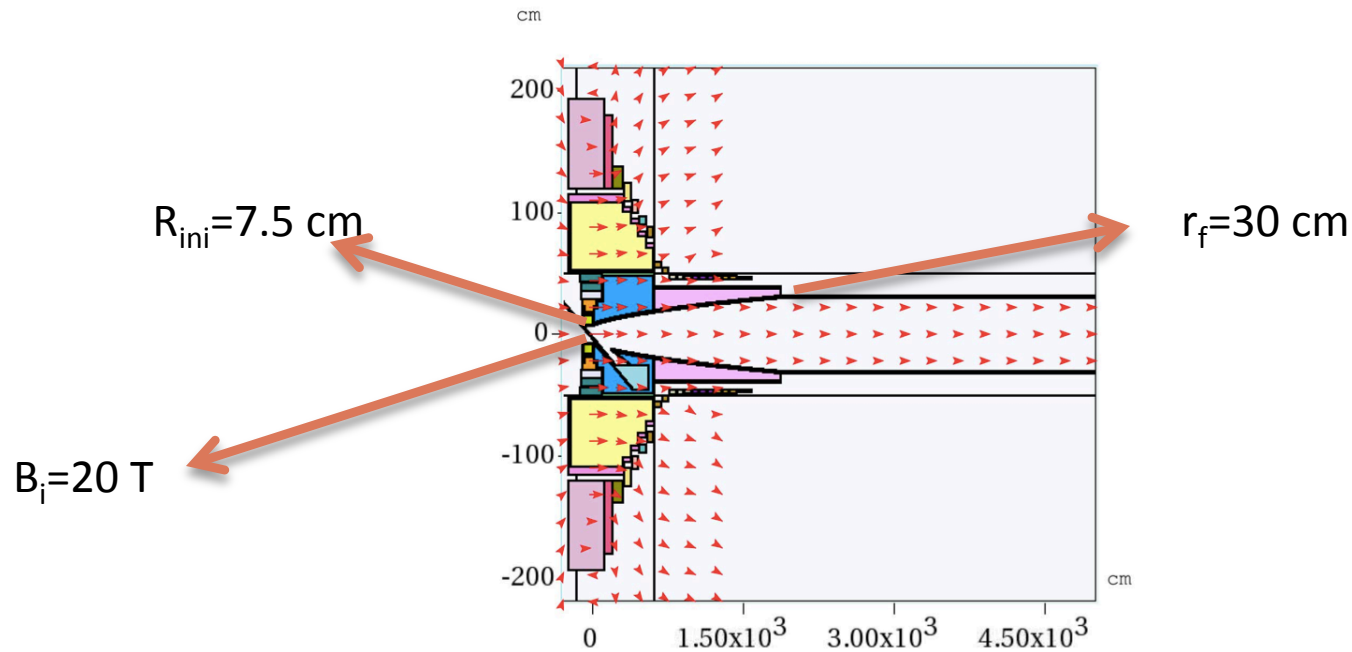
- Production of 10^{14} μ /s from 10^{15} p/s (\approx 4 MW proton beam)
- Low-energy π 's collected from side of long, thin cylindrical target
- Solenoid coils can be some distance from proton beam.
 - \geq 10-year life against radiation damage at 4 MW.
- Proton beam readily tilted with respect to magnetic axis.
 - \Rightarrow Beam dump (mercury pool) out of the way of secondary π 's and μ 's.
- Shielding of the superconducting magnets from radiation is a major issue.
 - Magnet stored energy \sim 3 GJ



5-T copper magnet insert; 10-T Nb₃Sn coil + 5-T NbTi outsert.
Desirable to eliminate the copper magnet (or replace by a 20-T HTS insert).

TARGET PARTICLE PRODUCTION WITH 15 T PEAK SOLENOID FIELD

- Particle-capture requirement ($P_t \leq 0.225 \text{ GeV}/c$)
 - $B \times r = 20 \text{ T} \times 7.5 \text{ cm} = 150 \text{ T-cm}$
 - $B \times r = 15 \text{ T} \times 10 \text{ cm} = 150 \text{ T-cm}$
- Fixed-flux requirement (Aperture requirement)
 - $B \times r^2 = 20 \times 7.5^2 = 1125 \text{ T-cm}^2$
 - $B \times r^2 = 15 \times 10^2 = 1500 \text{ T-cm}^2$
- MARS simulations with 15-T peak field & new aperture settings (taper radius $r = 30 \text{ cm}$ at all z)



Particle loss due to scrapping with beam pipe !

CURRENT TARGET OPTIMIZED PARAMETERS

(X. Ding et al.)

➤ Hg Target

- $\theta_{\text{Target}}=0.137$ rad
- $R_{\text{Target}}=0.404$ cm

➤ Proton Beam

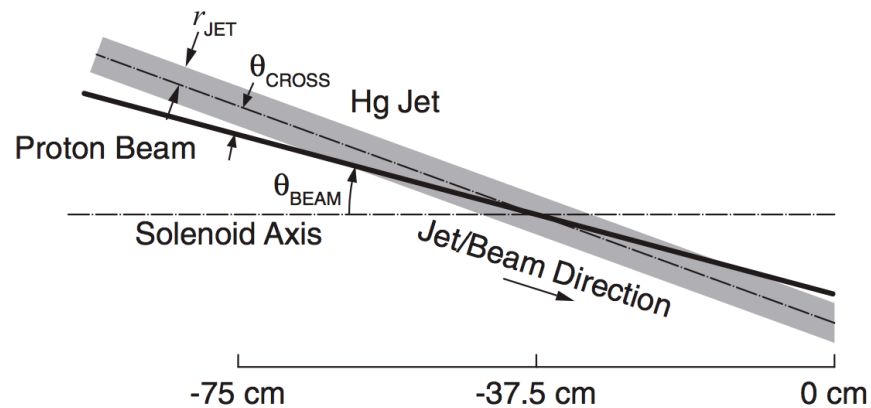
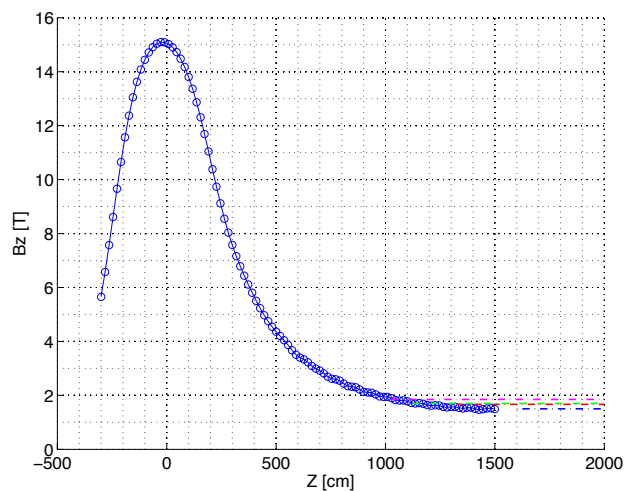
- $E=8$ GeV
- $\theta_{\text{Beam}}=0.117$ rad
- $\sigma_x=\sigma_y=0.1212$ cm (Gaussian Distribution)

➤ Solenoid Field

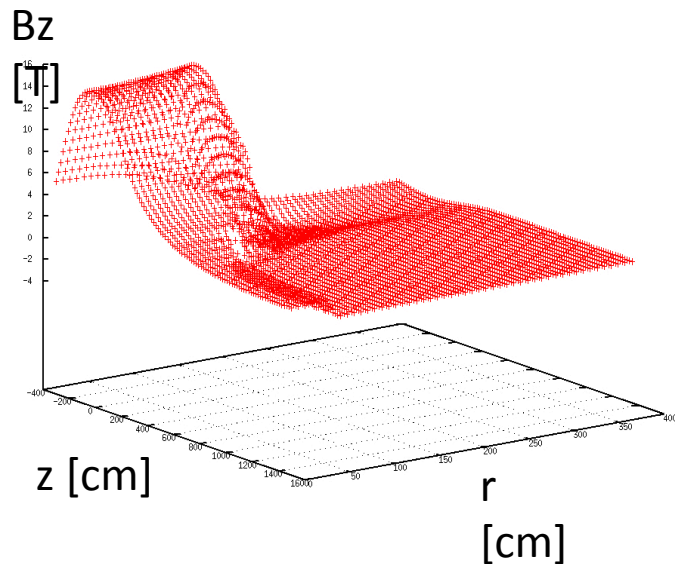
- IDS120h \rightarrow 20 T peak field at target position ($Z=0$)
- Aperture at Target $R=7.5$ cm - End aperture $R = 30$ cm
- Fixed Field $Z = 1862.0 \rightarrow B_z=1.5$ T

➤ Production: Muons within energy KE cut 40-180 MeV

➤ 3.27×10^4 ($N_{\text{ini}}=10^5$)



IDS120H



ANALYTIC FORM FOR TAPERED SOLENOID

Inverse-Cubic Taper

$$B_z(0, z_i < z < z_f) = \frac{B_1}{[1 + a_1(z - z_1) + a_2(z - z_1)^2 + a_3(z - z_1)^3]^p}$$

$$a_1 = -\frac{B_1'}{pB_1} \quad a_2 = 3\frac{(B_1/B_2)^{1/p} - 1}{(z_2 - z_1)^2} - \frac{2a_1}{z_2 - z_1}$$

$$a_3 = -2\frac{(B_1/B_2)^{1/p} - 1}{(z_2 - z_1)^3} + \frac{a_1}{(z_2 - z_1)^2}$$

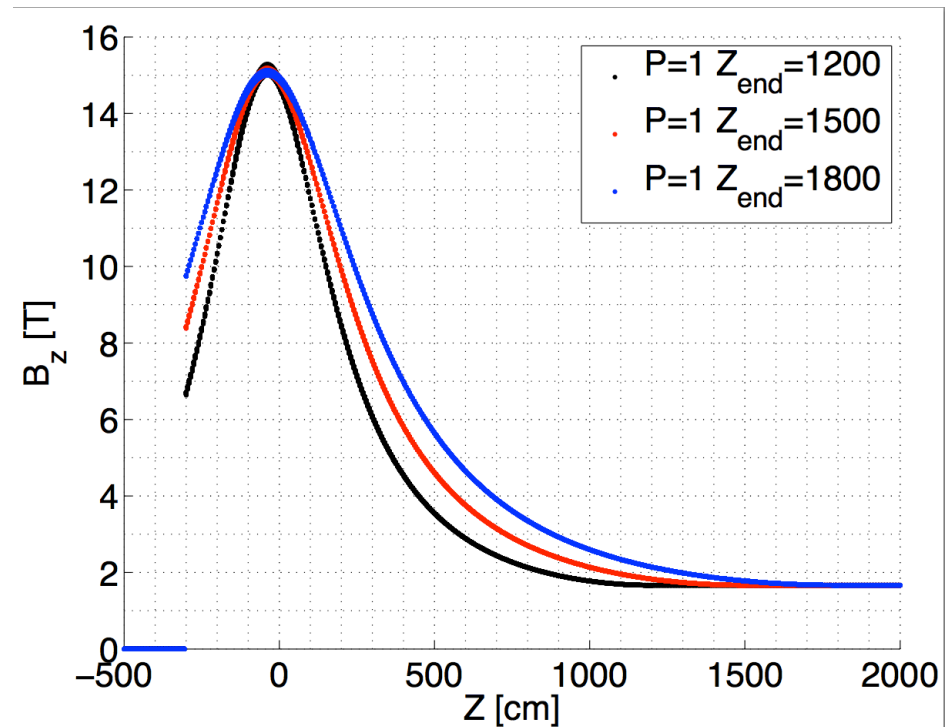
Off-axis field approximation

$$B_z(r, z) = \sum_n (-1)^n \frac{a_0^{(2n)}(z)}{(n!)^2} \left(\frac{r}{2}\right)^{2n}$$

$$B_r(r, z) = \sum_n (-1)^{n+1} \frac{a_0^{(2n+1)}(z)}{(n+1)(n!)^2} \left(\frac{r}{2}\right)^{2n+1}$$

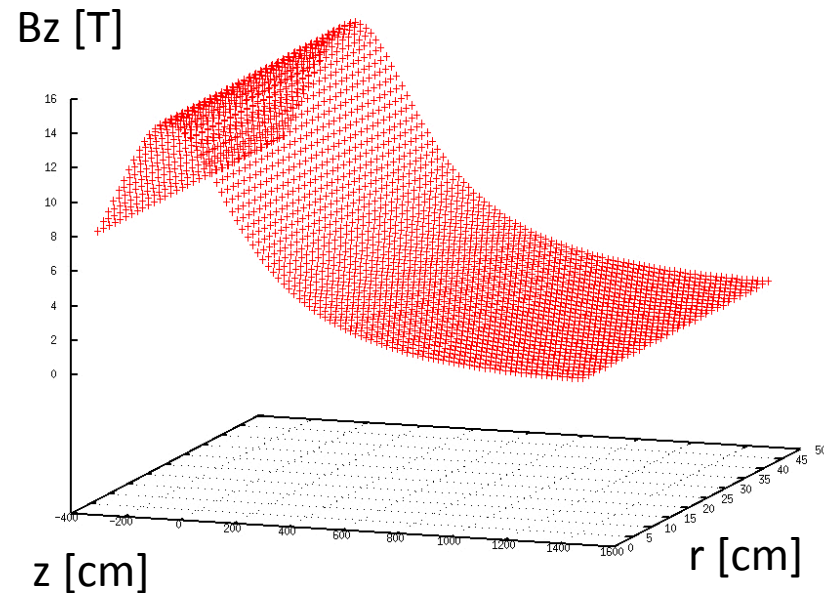
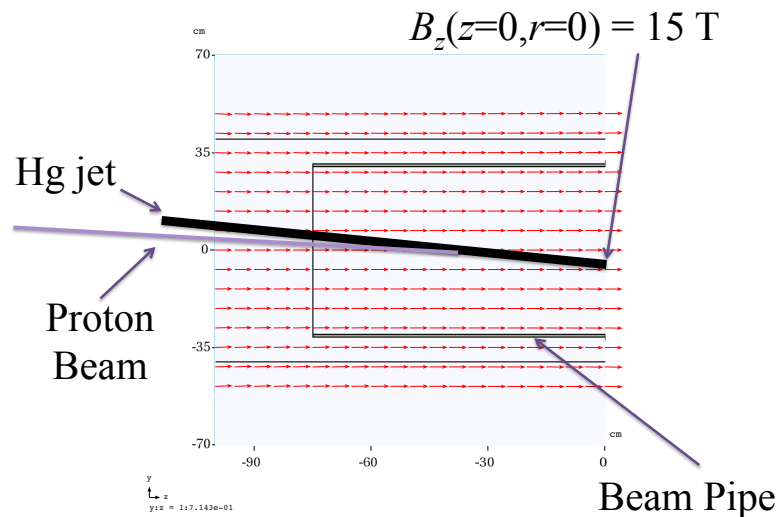
$$a_0^{(n)} = \frac{d^n a_0}{dz^n} = \frac{d^n B_z(0, z)}{dz^n}$$

Field at R=0



MARS SIMULATION SETUP

- Beam Pipe with constant $R=30$ cm (eliminate particle loss due to scrapping)
- Beam Pipe material changed to balckhole to speed calculations
- Added subroutine to m1510.f (FIELD K. McDonald) to calculate the field using inverse cubic equations
- $N_{\text{proton}}=5 \times 10^5$
- Store particles information at $z=0$
- Select $(\mu^+ - k^+ - \pi^+)$



PARTICLE TRACKING THROUGH FRONT END

1- Taper solenoid field with different settings

$B_z(r=0)$ 20 \rightarrow 1.5 T Taper Length 8 \rightarrow 43 m

$B_z(r=0)$ 15 \rightarrow 1.5 T Taper Length 8 \rightarrow 43 m

$B_z(r=0)$ 15 \rightarrow 1.8 T Taper Length 8 \rightarrow 43 m

$B_z(r=0)$ 15 \rightarrow 2.0 T Taper Length 8 \rightarrow 43 m

2- ICOOL applied aperture for decay region $R_{\text{aperture}} = 0.4$ m & 0.3 m to end

3- Good particles are those who satisfy the following conditions/cuts

1- Survived the phase rotator and cooling sections

2- Fall within required acceleration acceptance cuts

- $0.1 < P_z < 0.3$ GeV

- Transverse cut $R < 0.3$ m

- Longitudinal cut 0.15 m

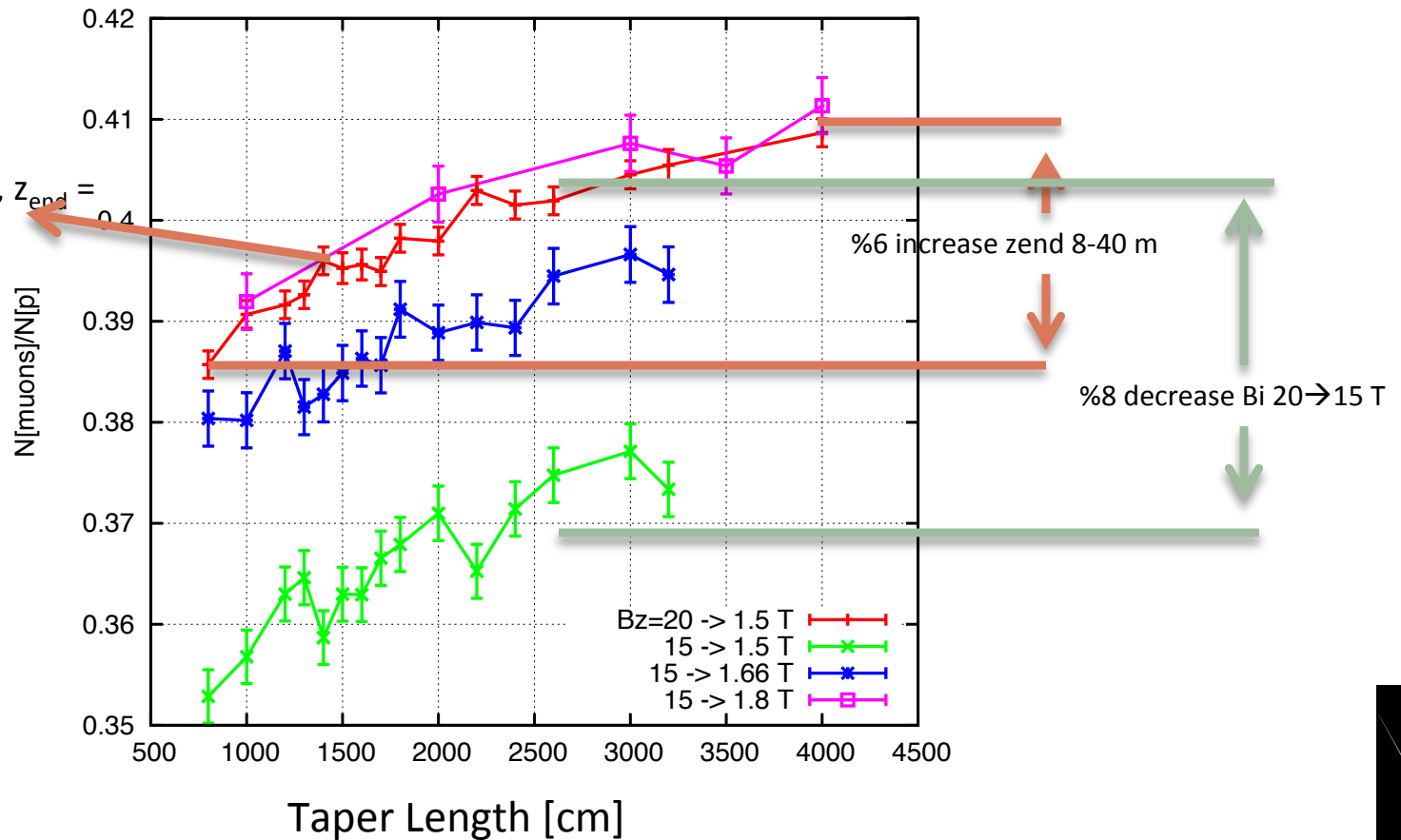
MARS SIMULATION RESULTS

Tapered field using inverse-cubic field ($P = 1$)

Mesons count at $z=50$ m with K.E. 40-180 MeV

Present baseline:

$B_i = 20$ T, $B_f = 1.5$ T, $z_{end} = 15$ m.

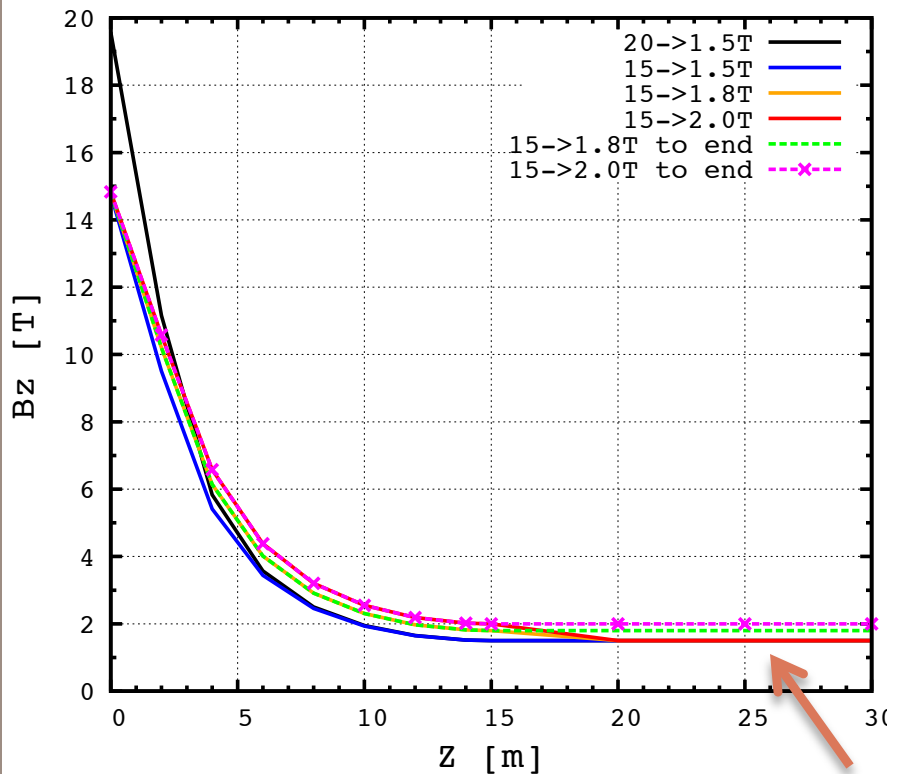


MUON COUNT AT END OF "FRONTEND"

Muons within required acceleration acceptance cuts after cooling section

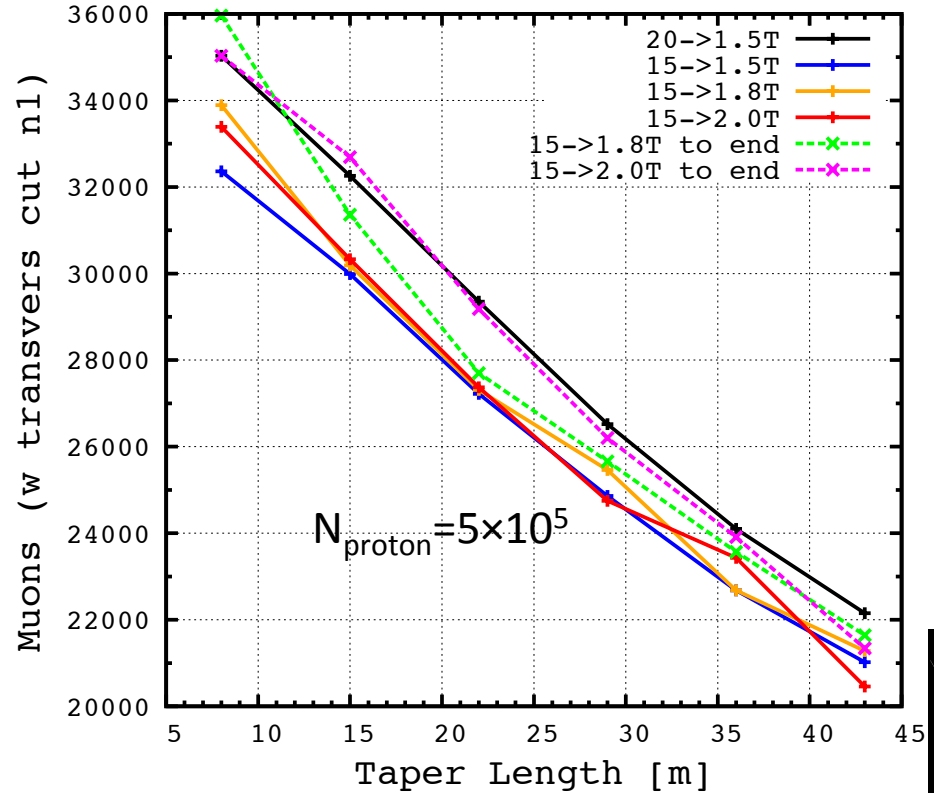
- $0.1 < P_z < 0.3$ GeV
- Transverse cut $R < 0.3$ m
- Longitudinal cut 0.15 m

Solenoid Field along z-axis



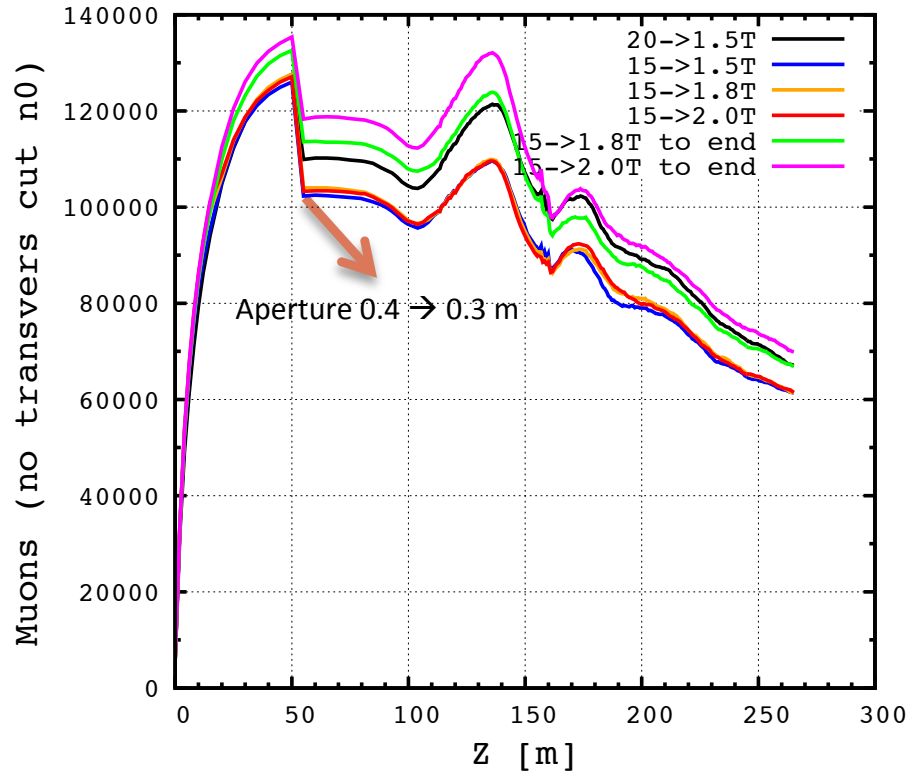
1.5 T

Shorter taper better survive buncher
- phase rotator & cooling

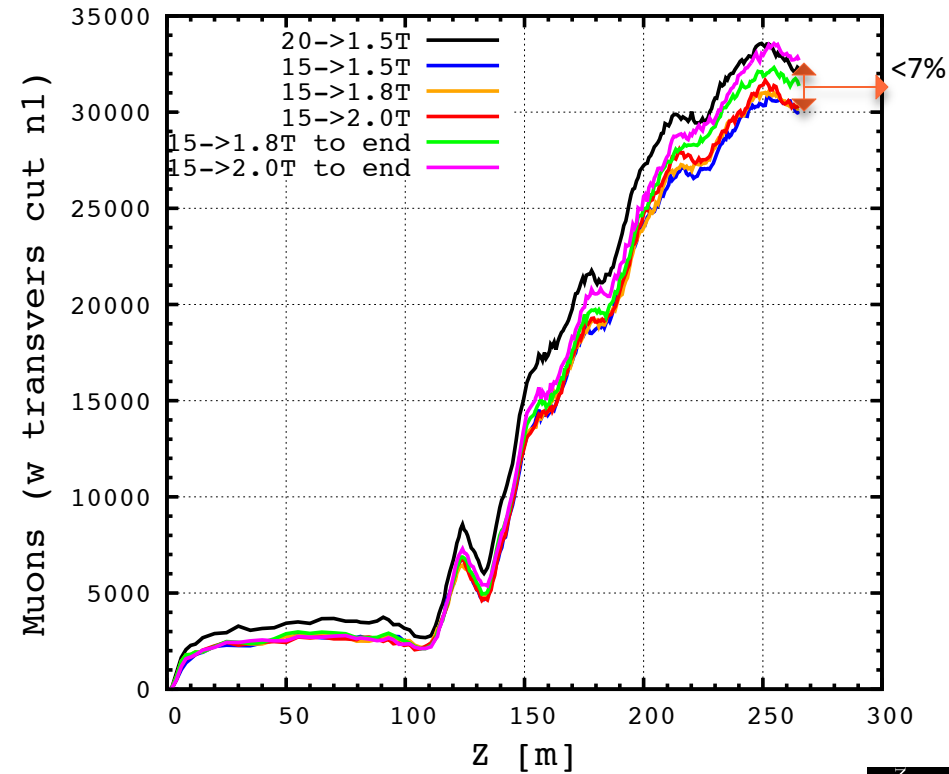


TRANSMISSION THROUGH FRONT END

Pz & Σ cut



Trans, Pz, & Σ cut

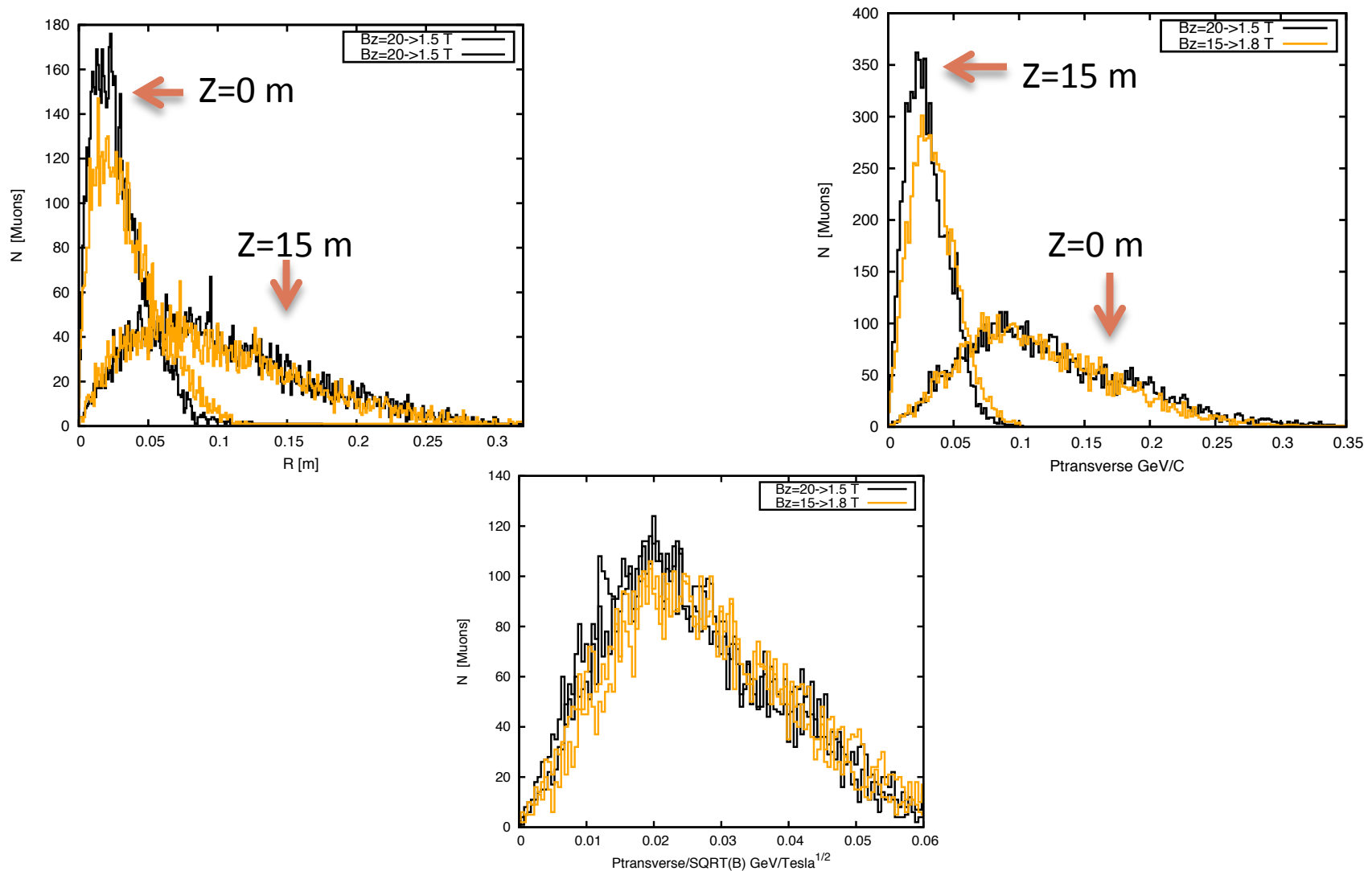


DISTRIBUTIONS OF PARTICLES SURVIVED THE FRONT END AND ACCELERATION CUTS

- 1- Taper solenoid field: 20 → 1.5 T over 15 m
- 2- ICOOL applied aperture for decay region $R_{\text{aperture}} = 0.4 \text{ m}$ & 0.3 afterwards
- 3- Good particles are those who satisfy the following conditions/cuts
 - 1- Survived the phase rotator and cooling sections
 - 2- Fall within required acceleration acceptance cuts
 - $0.1 < P_z < 0.3 \text{ GeV}$
 - Transverse cut $R < 0.3 \text{ m}$
 - Longitudinal cut 0.15 m

DISTRIBUTIONS OF PARTICLES SURVIVED THE FRONT END AND ACCELERATION CUTS

Particle distribution Taper Length =15 m



CONCLUSION

- Mesons count at 50 m increases with longer taper
- $B_z=15 \rightarrow 1.8T$ produces as much mesons counted at 50 m as $B_z=20 \rightarrow 1.5T$
- 15 T peak field case has $\sim 7\%$ less yield at end of cooling though it produces about the same number of muons at the target.
- No clear mismatch in the lattice that shows huge particle loss
- Particle radii extends from 0.1 at $z=0$ to 0.3 m at $z=15$ m
- Particles transverse momenta extends from 0.3 at $z=0$ to 0.1 m at $z=15$ m

| Taper Length | End of Decay Channel $z=50$ m No cuts | End of FE $z=265$ m Eclac acceleration acceptance cuts |
|--------------|---|--|
| Short | | Better |
| Long | Better | |