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**NUCLEAR  
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Section A

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# Particle production for a muon storage ring

## I. Targetry and $\pi/\mu$ yield<sup>☆</sup>

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### Abstract

Efficient production and collection of a large number of muons is needed to make a neutrino factory based on a muon storage ring viable. Results of extensive MARS simulations for 2–30 GeV protons on various targets in a 20 T hybrid solenoid followed by a matching section and decay channel are reported. Part I describes pion and muon yields, targetry issues, and beam energy and power considerations. Part II describes radiation loads on targets, the capturing system and shielding. © 2001 Elsevier Science B.V. All rights reserved.

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### 1. Introduction

To achieve adequate parameters of a neutrino factory based on a muon storage ring [1], it is necessary to produce and collect large numbers of muons. The system starts with a proton beam impinging on a thick target kept in a high-field solenoid (20 T, 1-m long, aperture radius  $R_a = 7.5$  cm), followed by a 3-m long matching section and a solenoidal decay channel (1.25 T, 50–100 m in length,  $R_a = 30$  cm) which collects muons resulting from pion decay [2,3]. Optimization of beam, target and solenoid parameters were done over the years with the MARS code [4,5] for a  $\mu^+\mu^-$  collider project [2,3,6–9]. This paper focuses on parameters needed for a muon storage ring and

briefly describes the results of extensive MARS simulations of  $\pi/\mu$ -yield (Part I) and radiation fields in the target station and capturing system (Part II) for 2–30 GeV proton beams. Preliminary results were given in Refs. [1,9].

### 2. Captured $\pi/\mu$ beam vs. target and beam parameters

Realistic 3-D geometry together with material and magnetic field distributions based on the solenoid magnet design optimization have been implemented into MARS. Graphite (C) and mercury (Hg) tilted targets were studied. A two interaction length target (80 cm for C of radius  $R_T = 7.5$  mm and 30 cm for Hg of  $R_T = 5$  mm) is found to be optimal in most cases, keeping  $R_T \geq 2.5\sigma_{x,y}$ , where  $\sigma_{x,y}$  are the beam RMS spot sizes. The calculation model (Fig. 1), keeping the

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main features of the baseline design [8,9], has been significantly refined in the course of the study [1]. A deviation of  $B_z$  and  $B_r$  (Fig. 1 (right)) from the ideal field [8,9], results in the reduction of the  $\pi/\mu$ -yield in the decay channel by about 7% for C and by 10–14% for Hg targets.

Results of a detailed optimization of the particle yield  $Y$  are presented below, in most cases for a

sum of the numbers of  $\pi$  and  $\mu$  of a given sign and energy interval at a fixed distance  $z = 9$  m from the target. It turns out, that for proton energies  $E_p$  from a few GeV to about 30 GeV, the shape of the low energy spectrum of such a sum is energy-independent and peaks around  $E = 130$  MeV, where  $E$  is  $\pi/\mu$  kinetic energy (Fig. 2). Moreover, the sum is practically independent of  $z$  at  $z \geq$

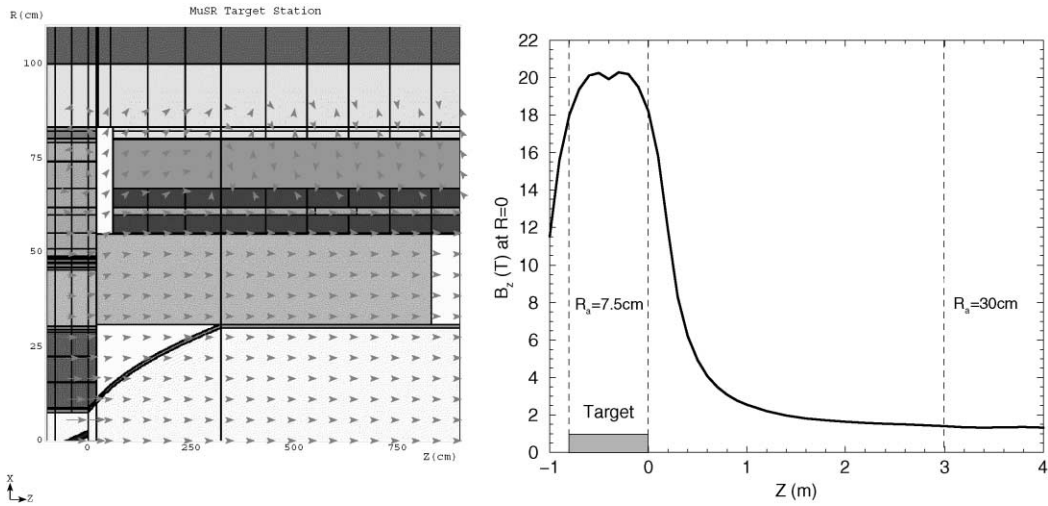


Fig. 1. MARS model of the target/solenoid system (left) and  $B_z$  field profile (right).

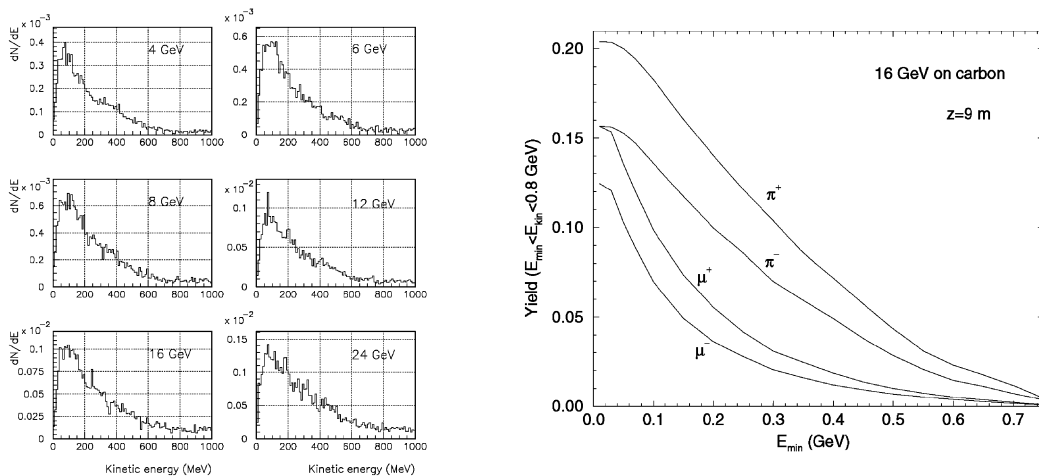


Fig. 2. Energy spectra of  $\pi^+ + \mu^+$  for 4–24 GeV protons (left) and numbers of particles in the  $(E_{min} - 0.8$  GeV) interval vs.  $E_{min}$  for 16 GeV protons (right) at  $z = 9$  m for a 80-cm C target ( $R_T = 7.5$  mm,  $\alpha = 50$  mrad).

9 m—confirming a good matching and capturing—with a growing number of muons and proportionally decreasing number of pions along the decay channel. For the given parameters, the interval of  $30 \text{ MeV} < E < 230 \text{ MeV}$  around the spectrum maximum is considered as the one to be captured by a phase rotation system.

The yield  $Y$  grows with the proton energy  $E_p$ , is almost material-independent at low energies and grows with target  $A$  at high energies, being almost a factor of two higher for Hg than for C at  $E_p = 16\text{--}30 \text{ GeV}$  (Fig. 3). To avoid absorption of spiraling pions by target material, the target and beam are tilted by an angle  $\alpha$  with respect to the

solenoid axis. The yield is higher by 10–30% for the tilted target. For a short Hg target,  $\alpha = 150 \text{ mrad}$  seems to be the optimum (Fig. 3), while  $\alpha = 50 \text{ mrad}$  is chosen in Ref. [1] for a long C target to locate a primary beam dump at 6 m from the target. Fig. 4 shows the dependence of the yield on Hg and C target radii under the baseline  $R_T = 2.5\sigma_{x,y}$  condition. Figs. 4 and 5 show that maximum yield occurs at target radius  $R_T = 7.5 \text{ mm}$  for C and  $R_T = 5 \text{ mm}$  for Hg targets with  $R_T = 3.5\sigma_{x,y}$  and  $4\sigma_{x,y}$  conditions for the beam spot size, respectively. The baseline criterion  $R_T = 2.5\sigma_{x,y}$  reduces the yield by about 10% for the graphite target, but is more

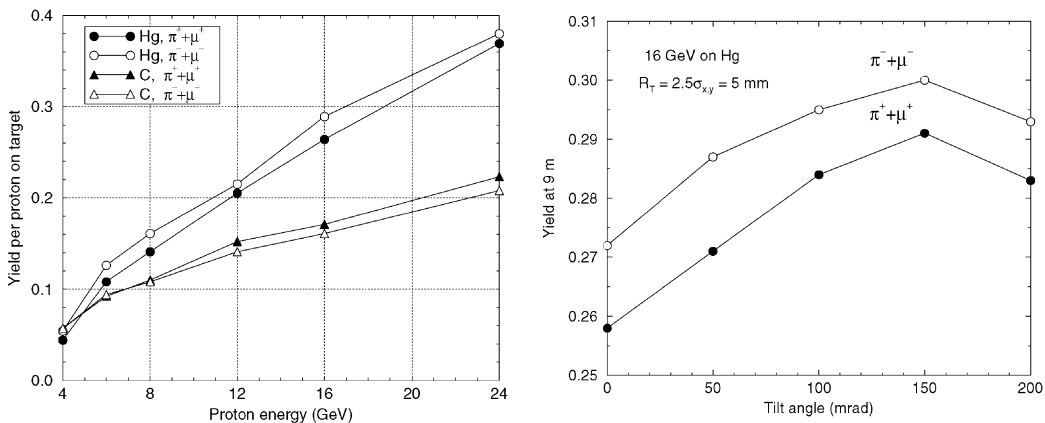


Fig. 3. Yield from Hg and C targets vs.  $E_p$  (left) and yield from a Hg target at  $E_p = 16 \text{ GeV}$  vs. tilt angle (right).

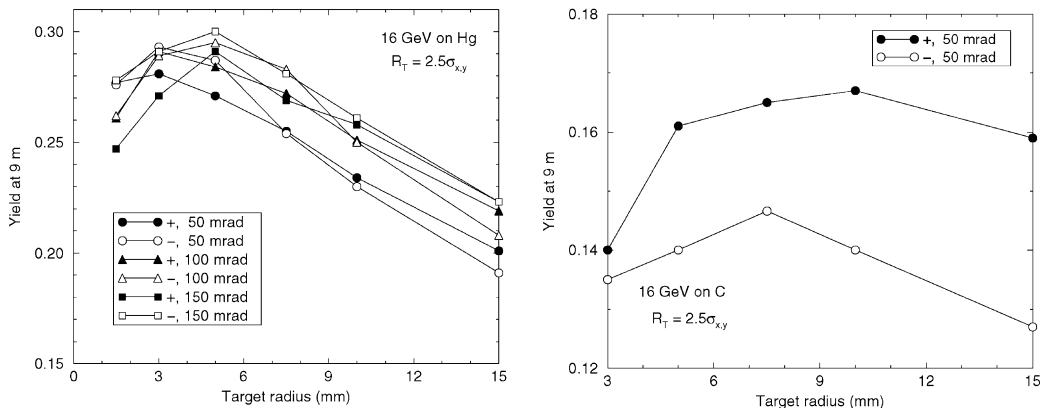


Fig. 4. Yield as a function of a target radius, Hg (left) and C (right), for a 16-GeV proton beam and several tilt angles.

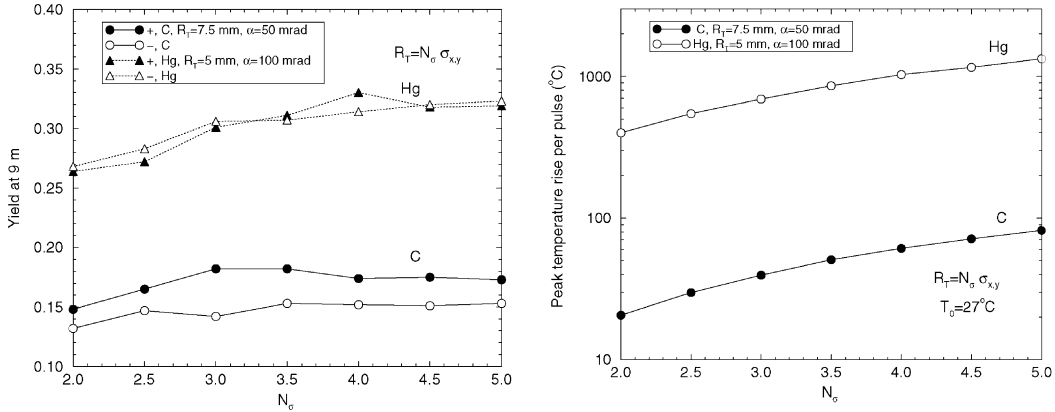


Fig. 5. Yield (left) and maximum instantaneous temperature rise (right) as a function of a target to a RMS beam spot size ratio (right).

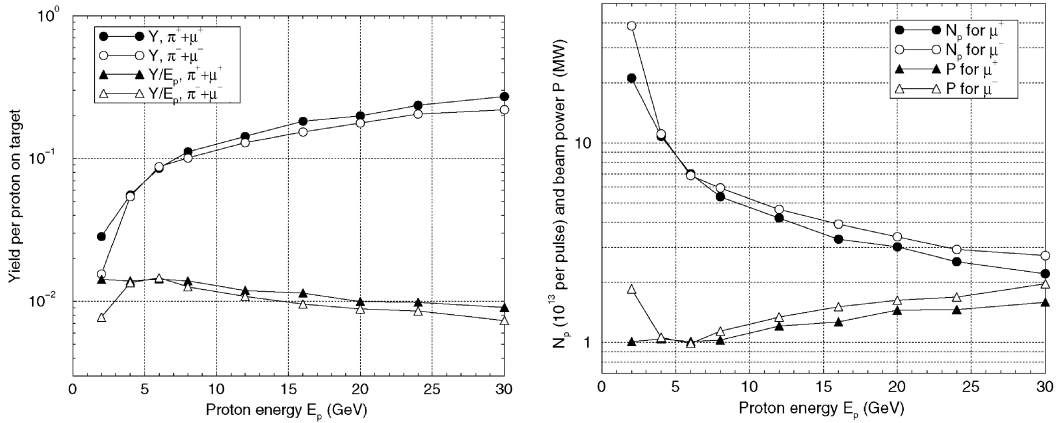


Fig. 6.  $Y$  and  $Y/E_p$  (left) and  $N_p$  and beam power (right) for C target.

optimal from the energy deposition point of view (Fig. 5).

The ratio of Hg to C yields varies with the beam energy, as well as with other beam/target parameters. At 16 GeV it is in the range 1.5–1.7 for positives and 1.7–2.2 for negatives. Optimizing beam/target parameters, it is found that the best results for the particle yield in the decay channel at 16 GeV with the given cut are:  $Y_{\pi^+\mu^+} = 0.182$  and  $Y_{\pi^-\mu^-} = 0.153$  for the 80-cm C target and  $Y_{\pi^+\mu^+} = 0.309$  and  $Y_{\pi^-\mu^-} = 0.315$  for the 30-cm Hg target, i.e., at 16 GeV (best Hg)/(best C)=1.7 (+) and 2.06 (–).

### 3. Beam power considerations

The yield per beam power is almost independent of  $E_p$  for high-Z targets at  $6 < E_p < 24$  GeV and drops by 30% at 16 GeV from a 6-GeV peak for graphite (Fig. 6 (left)). The higher  $E_p$  reduces the number of protons on the target, but results in more severe energy deposition in the target. To provide  $N_{\mu} = 2 \times 10^{20}$  muon decays per year in the straight section at 15 Hz, one needs to have  $6 \times 10^{12}$  muons per pulse in the decay channel assuming a factor of three total loss on the way from the decay channel to the ring. With that,

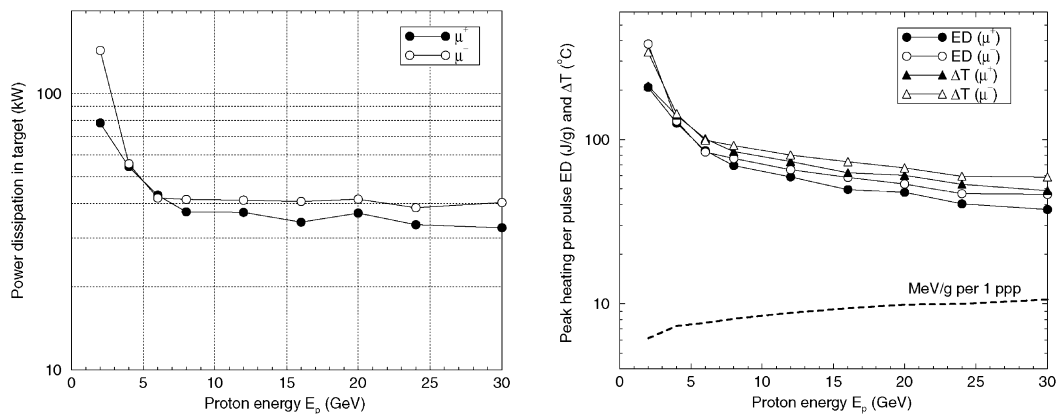


Fig. 7. Power dissipation in C target (left) and peak energy deposition and temperature rise in C target (right), providing  $N_{\mu} = 2 \times 10^{20}$  muon decays per year. A dashed line shows a peak energy deposition density per proton on target.

$3.30 \times 10^{13}$  and  $3.92 \times 10^{13}$  protons per pulse at 16 GeV on the optimal C target are needed for positives and negatives, respectively. This corresponds to 1.27 and 1.51 MW beams. For a Hg target, these numbers are 1.7 and 2.06 times lower. Fig. 6 (right) shows the required number of protons  $N_p$  and beam power as a function of  $E_p$  for the C target, while Fig. 7 presents power dissipation and peak heating in the C target to provide  $N_{\mu} = 2 \times 10^{20}$  muon decays per year. At 16 GeV, the peak instantaneous temperature rise is 60–70°C and power dissipation is 34.3 and 40.7 kW for the  $\mu^+$  and  $\mu^-$  modes, respectively. For Hg targets, the required beam power is lower, in the range 0.73–0.75 MW; however, the peak temperature rise per pulse is 750°C, because of higher energy deposition density.

#### 4. Conclusions

The number of muons required for a neutrino factory can be provided in the decay channel for further capturing by a phase rotation system with graphite and mercury targets impinged by intense 15-Hz proton beams in the energy range 2–30 GeV. Depending on proton energy, the required beam power is 1–2 MW with a graphite target, and 0.7–1 MW with a mercury target. The results obtained in the course of thorough MARS

simulations provide a basis for further optimization of the target/capture system.

#### References

- [1] N. Holtkamp, D. Finley (Eds.), A Feasibility Study of a Neutrino Source Based on a Muon Storage Ring, Fermilab-Pub-00/108-E, 2000.
- [2] N.V. Mokhov, R.J. Noble, A. Van Ginneken, Target and collection optimization for muon colliders, in: J.C. Gallardo (Ed.), Proceedings of the 9th Advanced ICFA Beam Dynamics Workshop, Montauk, NY, 1995, pp. 61–86, Fermilab-Conf-96/006, 1996.
- [3]  $\mu^+ \mu^-$  Collider Feasibility Study BNL-52503, Fermilab-Conf-96/092, LBNL-38946, 1996.
- [4] N.V. Mokhov, The MARS Code System User's Guide, Fermilab-FN-628, 1995; N.V. Mokhov, et al., MARS Code Developments, Fermilab-Conf-98/379, 1998; <http://www-ap.fnal.gov/MARS/>.
- [5] N.V. Mokhov, MARS code developments, benchmarking and applications, in: Proceedings of ICRS-9 International Conference on Radiation Shielding, Tsukuba, Ibaraki, Japan, 1999, J. Nucl. Sci. Tech. 1 (2000) 167–171, Fermilab-Conf-00/066, 2000.
- [6] D. Ehrst, N.V. Mokhov, R.J. Noble, A. Van Ginneken, Target options and yields for a muon collider source, in: M. Comyn, M.K. Craddock, M. Reiser, J. Thomson (Eds.), Proceedings of the 1997 Particle Accelerator Conference, Vancouver, BC, Canada, 1997, pp. 393–395.
- [7] C.M. Ankenbrandt, et al., Phys. Rev. ST Accel. Beams 2 (1999) 081001; C.M. Ankenbrandt, et al., Fermilab-Pub-98/179, 1999.

- [8] R.J. Weggel, N.V. Mokhov, Pion yield vs. geometry of target and 20-T pulse solenoid for a muon collider experiment, in: A. Luccio, W. MacKay (Eds.), Proceedings of the 1999 Particle Accelerator Conference, New York City, 1999, pp. 3047–3049; BNL-66256 (1999).
- [9] N.V. Mokhov  $\pi/\mu$  Yield and Power Dissipation for Carbon and Mercury Targets in 20-Tesla Solenoid with Matching Section, Mucool Note-MUC0061 (1999), <http://www-ap.fnal.gov/~mokhov/mumu/target99/muc0061> and updates there.